

Railway Project

Rio Negro RAILWAY BRIDGE CALCULATION REPORT

DOCUMENT APPROVAL

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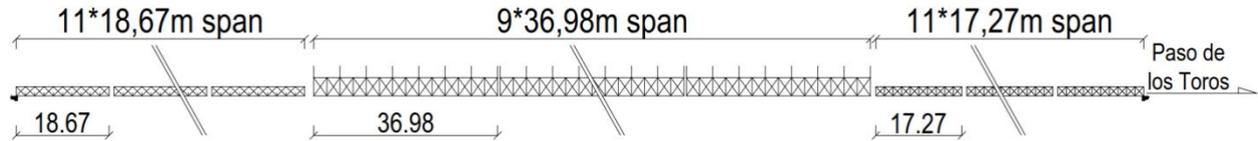
REVISION HISTORY

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1 SCOPE

Rio Negro Bridge consists of three different types of cross sections and three different span lengths. Total length of the bridge is 704 m; consisting of 11x 18,67 m spans, 9x 37 m spans and 11x 17,27 m spans.



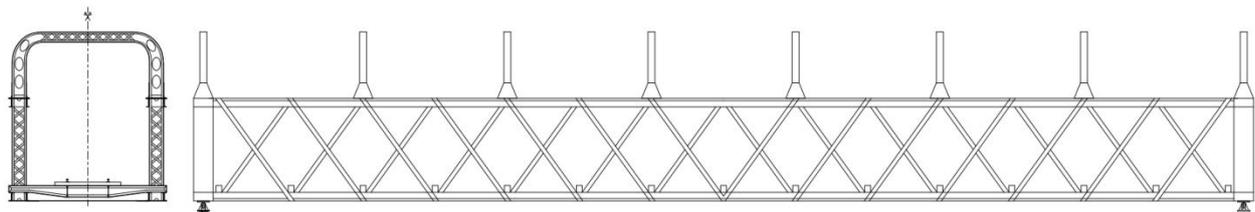
Picture 1, Rio Negro bridge side view

This report describes the design criteria and capacity of the old structure. Also, the utilizations for the new structures are shown. The chosen solution in pre-engineering is based on experience that the main trusses have capacity, but the secondary structures (cross-girders and longitudinal beams) are problematic mainly in the capacity, fatigue, and functionality of the joints. The known problems of these types of bridges are illustrated in document IRS 77802 (former UIC 778-2) Recommendations for determining the carrying capacity and fatigue risks of existing metallic railway bridges.

This calculation report is a summary of all calculations executed with FEM-modeling and Structural Analysis and calculations. Its purpose is to show all selections made by the engineer and show the results of the analysis.

1.1 37 m Lattice/Truss Bridge

The main goal of this calculation is to show that the old truss structures can be utilized from existing 52,0 m truss sections of the bridge. The main load bearing lattice/truss will be saved as they are and cross beams and longitudinal rail supporting beams will be renewed. There is a possibility to strengthen most critical profiles of truss if more detailed calculations and decisions in the detailed design phase require more safety margins.

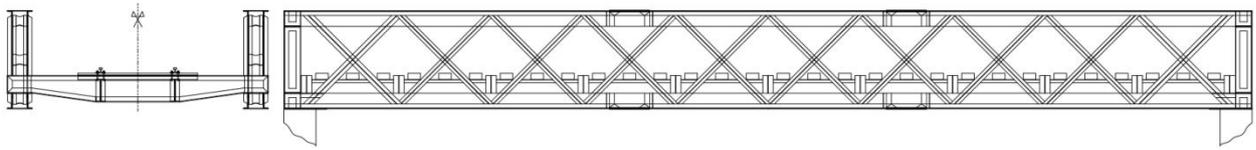


Picture 2, Rio Negro Bridge 37 m

1.2 18,67 m Truss Bridge

The main goal of this calculation is to show that the old truss structures could be utilized from existing 19 m truss sections of the bridge.

The girder bridge of 19 m span was studied with same actions as the truss sections with replacing of cross beams and longitudinal rail supporting beams. But technical and economical evaluations show that it is more cost effectiveness that all girders spans will be renewed completely. The lifting weight of a single span is suitable for this kind of replacement. The pre-engineering solution is to replace these spans.

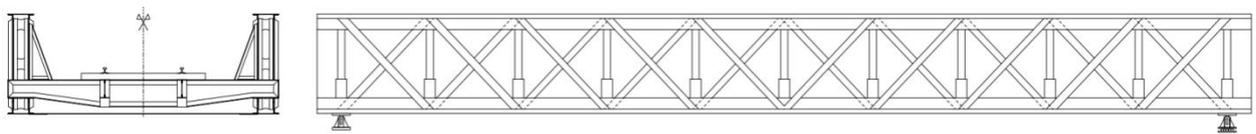


Picture 3, Rio Negro Bridge 19 m

1.3 17 m Truss Bridge

The main goal of this calculation is to show that the old truss structures could be utilized from existing 17 m truss sections of the bridge.

The girder bridge of 17 m span was studied with same actions as the truss sections with replacing of cross beams and longitudinal rail supporting beams. But technical and economical evaluations show that it is more cost effectiveness that all girders spans will be renewed completely. The lifting weight of a single span is suitable for this kind of replacement. The pre-engineering solution is to replace these spans.



Picture 4, Rio Negro 17 m

2 DESIGN CRITERIA

FEM calculations was made with Autodesk® Robot™ Structural Analysis Professional, Version 30.0.0.5913.

2.1 Structure

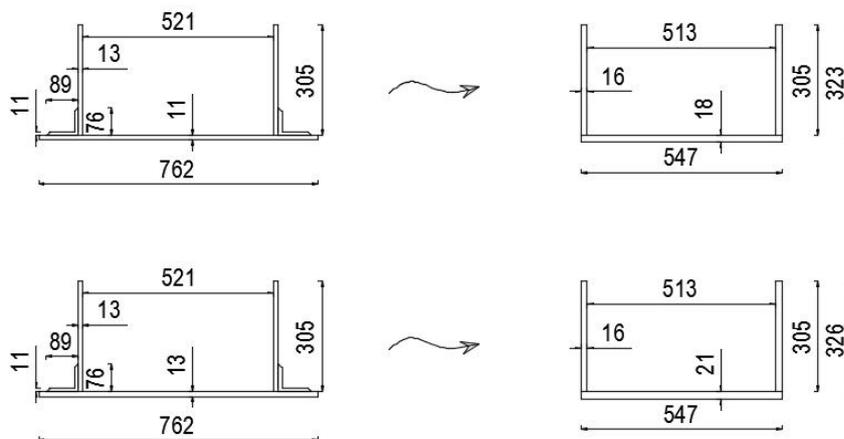
Bridge super structure members are complicated profiles of angles and plates with rivet connection. For building a FEM-model, simplified profiles were used. Simplifications were made so that function in FEM model equals actual profiles. The simplifications are shown in pictures 6-24 in section 2.1.1.

The calculations are based on an estimated geometry from insufficient quality old drawings, photos and limited site visit information. Before making final design, all structures need to be verified on site in order to gather the missing data.

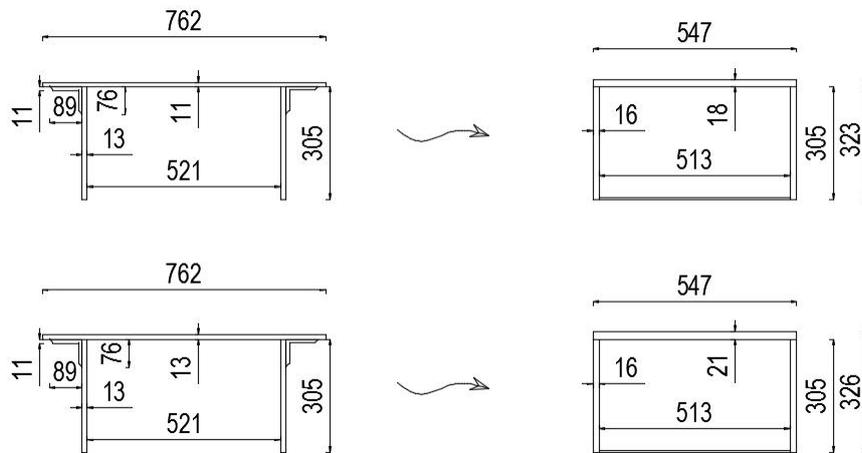


Picture 5, Rio Negro inside view

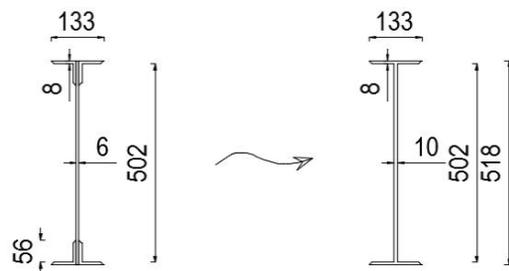
2.1.1 Simplifications for sections in 37 m span bridge



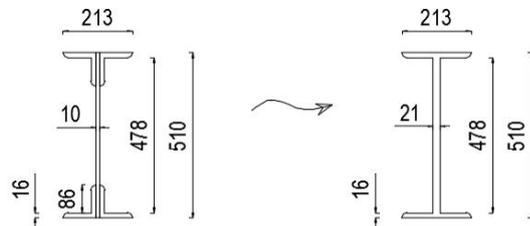
Picture 6, Lower main girder



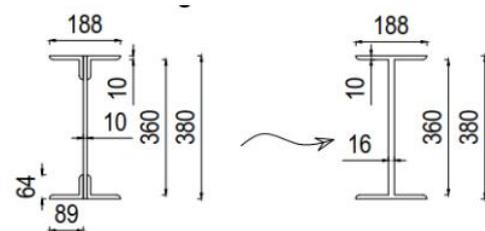
Picture 7, Upper main girder, type 1



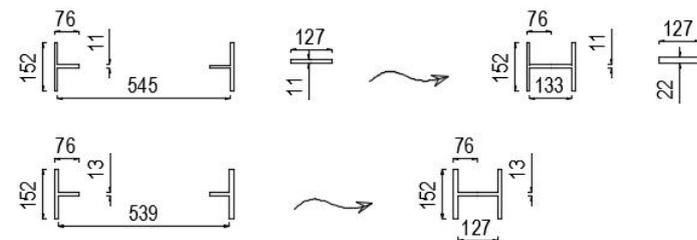
Picture 8, Longitudinal girder



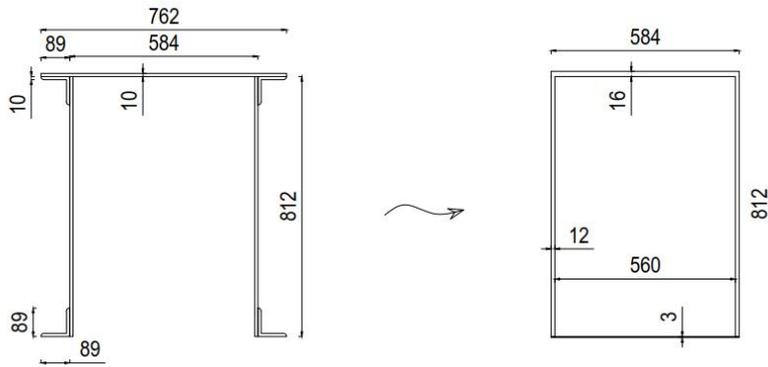
Picture 9, Cross girder



Picture 10, Upper cross bracing

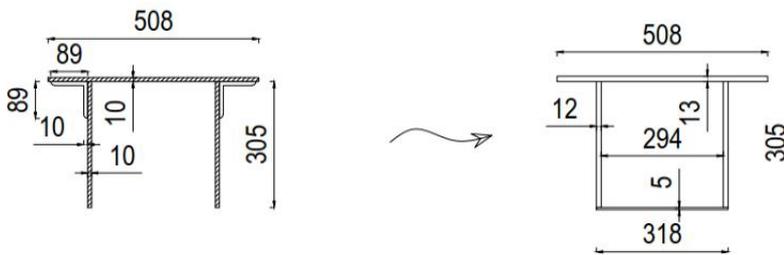


Picture 11, Diagonals

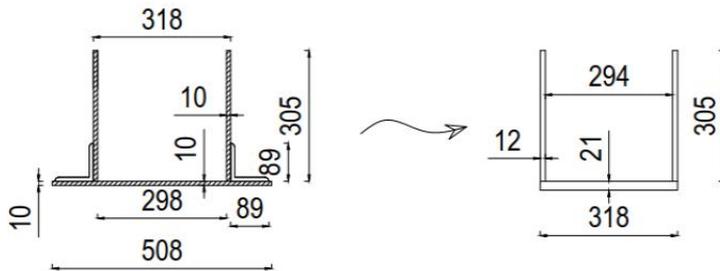


Picture 12, End frame

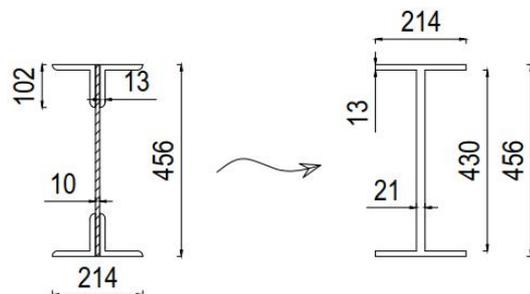
2.1.2 Simplifications for sections in 18,67 m span bridge



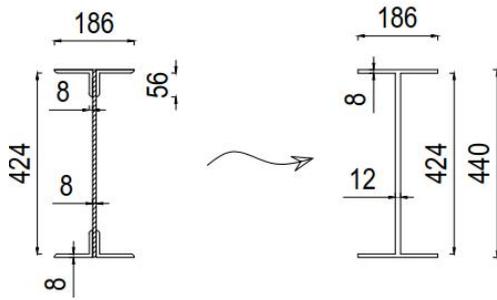
Picture 13, Upper main girder



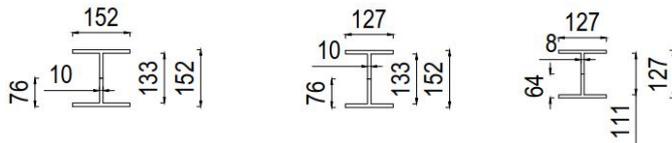
Picture 14, Lower main girder



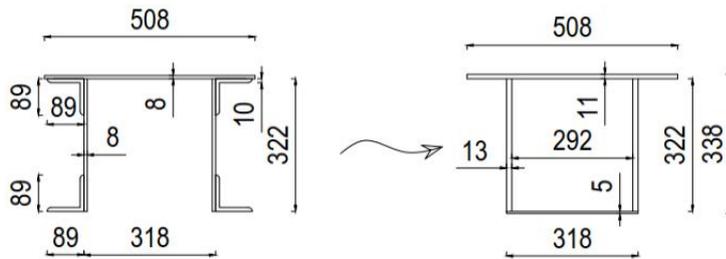
Picture 15, Cross girder



Picture 16, Longitudinal girder

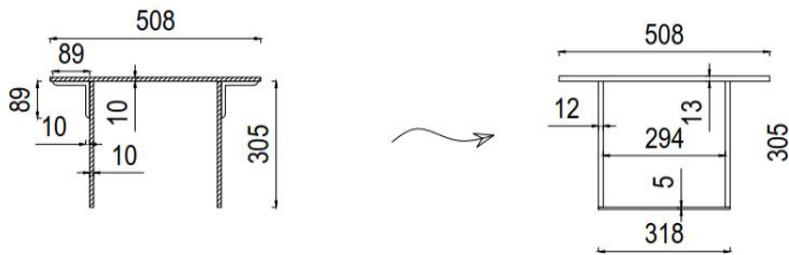


Picture 17, Diagonals, 3 types

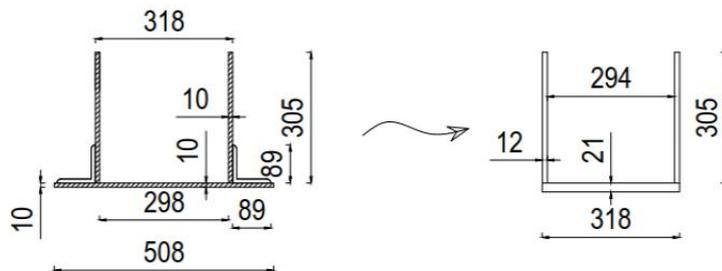


Picture 18, End frame

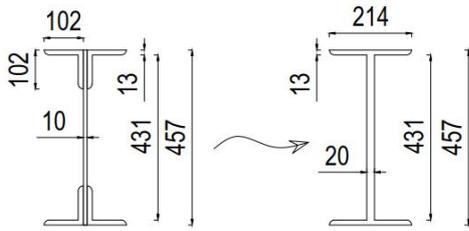
2.1.3 Simplifications for sections in 17 m span bridge



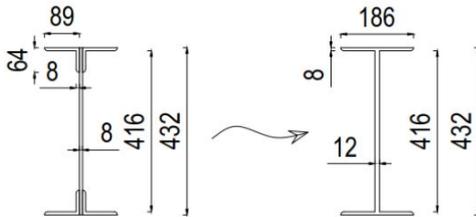
Picture 19, Upper main girder



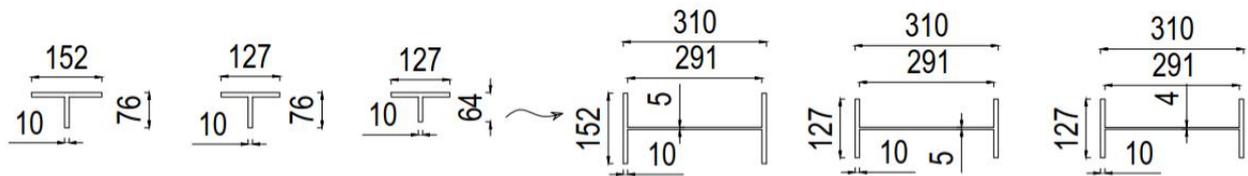
Picture 20, Lower main girder



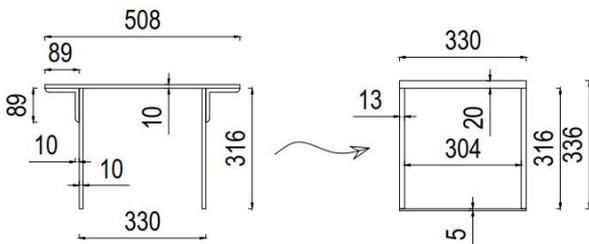
Picture 21, Cross girder



Picture 22, Longitudinal girder



Picture 23, Diagonals, 3 types



Picture 24, End frame

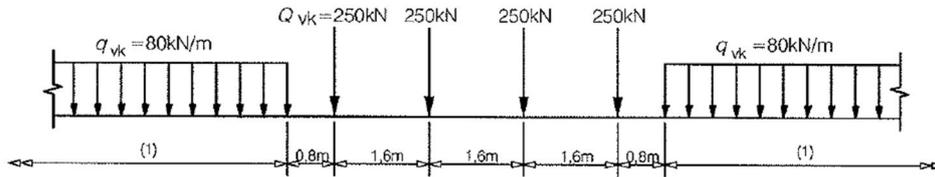
2.2 Loads

2.2.1 Selfweight / dead load

The Robot Structural Analysis gives weights of structures according to cross sections and selected materials. For the weight of steel is used 7850kg/m³. An additional 1kN/m² was added for the whole bridge area to act as weight of rails structures.

2.2.2 Train load

Train axle load is increased to 22,5 tons. Load is applied according to EN 1991-2, section 6.3.2, load model LM71.



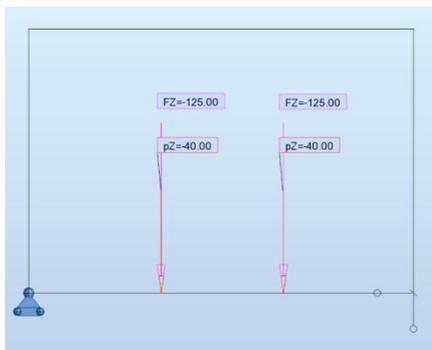
Key
 (1) No limitation

Picture 25, Train load model 71

In the calculations, the trains were placed on all locations on the bridge. The load can be anywhere on the bridge. The most critical locations of the traffic load are in the middle of the span and at the ends.



Picture 26, Load model 71 applications – side view (37m span bridge)

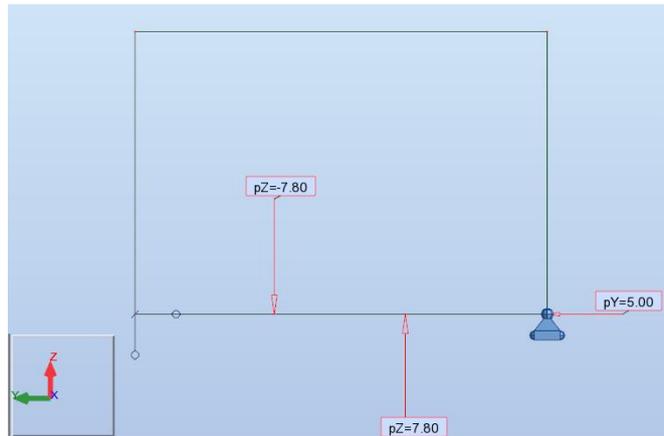
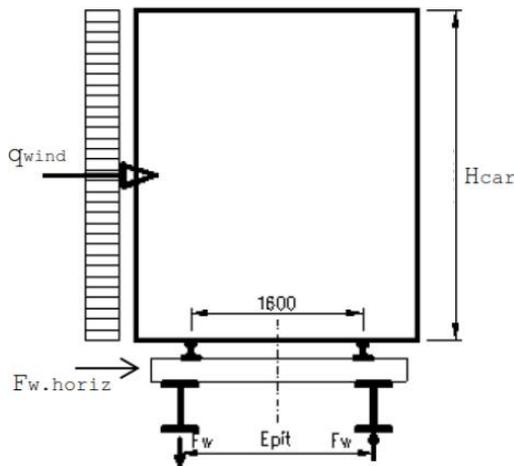


Picture 27, Load model 71 applications – front view

2.2.3 Wind load

The applied characteristic wind load is 1 kN/m^2 .

The wind effected area in truss bridges is minimal compared to the train area, so wind load is applied for the train cars for the whole length of the bridge.



Picture 28, Wind load

The most critical case for strains in structures is if bridge will be fully loaded at the same time with the wind. Structurally there is no such change that would make bridge behave differently from the last 100 years.

2.3 Load Combinations and combination factors

Load combinations are applied according to EN 1990, table A2.4

[AC> Table A2.4(A) Design values of actions (EQU) (Set A)

Persistent and transient design situation	Permanent actions		Prestress	Leading variable action (*)	Accompanying variable actions (*)	
	Unfavourable	Favourable			Main (if any)	Others
(Eq. 6.10)	$\gamma_{G,j,sup} G_{k,j,sup}$	$\gamma_{G,j,inf} G_{k,j,inf}$	$\gamma_P P$	$\gamma_{Q,1} Q_{k,1}$		$\gamma_{Q,i} \psi_{0,i} Q_{k,i}$

(*) Variable actions are those considered in Tables A2.1 to A2.3.

NOTE 1 The γ values for the persistent and transient design situations may be set by the National Annex.

For persistent design situations, the recommended set of values for γ are:

$\gamma_{G,sup} = 1,05$
 $\gamma_{G,inf} = 0,95^{(1)}$
 $\gamma_Q = 1,35$ for road and pedestrian traffic actions, where unfavourable (0 where favourable)
 $\gamma_Q = 1,45$ for rail traffic actions, where unfavourable (0 where favourable)
 $\gamma_Q = 1,50$ for all other variable actions for persistent design situations, where unfavourable (0 where favourable).
 γ_P = recommended values defined in the relevant design Eurocode.

For transient design situations during which there is a risk of loss of static equilibrium, $Q_{k,1}$ represents the dominant destabilising variable action and $Q_{k,i}$ represents the relevant accompanying destabilising variable actions.

During execution, if the construction process is adequately controlled, the recommended set of values for γ are:

$\gamma_{G,sup} = 1,05$
 $\gamma_{G,inf} = 0,95^{(1)}$
 $\gamma_Q = 1,35$ for construction loads where unfavourable (0 where favourable)
 $\gamma_Q = 1,50$ for all other variable actions, where unfavourable (0 where favourable)

(1) Where a counterweight is used, the variability of its characteristics may be taken into account, for example, by one or both of the following recommended rules:

- applying a partial factor $\gamma_{G,inf} = 0,8$ where the self-weight is not well defined (e.g. containers);
- by considering a variation of its project-defined position specified proportionately to the dimensions of the bridge, where the magnitude of the counterweight is well defined. For steel bridges during launching, the variation of the counterweight position is often taken equal to ± 1 m.

NOTE 2 For the verification of uplift of bearings of continuous bridges or in cases where the verification of static equilibrium also involves the resistance of structural elements (for example where the loss of static equilibrium is prevented by stabilising systems or devices, e.g. anchors, stays or auxiliary columns), as an alternative to two separate verifications based on Tables A2.4(A) and A2.4(B), a combined verification, based on Table A2.4(A), may be adopted. The National Annex may set the γ values. The following values of γ are recommended:

$\gamma_{G,sup} = 1,35$
 $\gamma_{G,inf} = 1,25$
 $\gamma_Q = 1,35$ for road and pedestrian traffic actions, where unfavourable (0 where favourable)
 $\gamma_Q = 1,45$ for rail traffic actions, where unfavourable (0 where favourable)
 $\gamma_Q = 1,50$ for all other variable actions for persistent design situations, where unfavourable (0 where favourable)
 $\gamma_Q = 1,35$ for all other variable actions, where unfavourable (0 where favourable) provided that applying $\gamma_{G,inf} = 1,00$ both to the favourable part and to the unfavourable part of permanent actions does not give a more unfavourable effect.

Combination factors according to EN 1990, Table A2.3.

Table A2.3 Recommended values of ψ factors for railway bridges

Actions			ψ_0	ψ_1	ψ_2 ⁴⁾
Main traffic actions (groups of loads)	gr11 (LM71 + SW/0)	Max. vertical 1 with max. longitudinal	0,80	0,80	0
	gr12 (LM71 + SW/0)	Max. vertical 2 with max. transverse			
	gr13 (Braking/traction)	Max. longitudinal			
	gr14 (Centrifugal/hosing)	Max. lateral			
	gr15 (Unloaded train)	Lateral stability with "unloaded train"			
	gr16 (SW/2)	SW/2 with max. longitudinal			
	gr17 (SW/2)	SW/2 with max. transverse			
	gr21 (LM71 + SW/0)	Max. vertical 1 with max. longitudinal			
	gr22 (LM71 + SW/0)	Max. vertical 2 with max. transverse			
	gr23 (Braking/traction)	Max. longitudinal			
	gr24 (Centrifugal/hosing)	Max. lateral			
	gr26 (SW/2)	SW/2 with max. longitudinal			
	gr27 (SW/2)	SW/2 with max. transverse			
gr31 (LM71 + SW/0)	Additional load cases	0,80	0,60	0	
Other operating actions	Aerodynamic effects		0,80	0,50	0
	General maintenance loading for non public footpaths		0,80	0,50	0
Wind forces ²⁾	F_{Wk}		0,75	0,50	0
	F_W^{**}		1,00	0	0
	T_k		0,60	0,60	0,50
Thermal actions ³⁾			0,8	–	0
Snow loads	$Q_{Sn,k}$ (during execution)		0,8	–	0
Construction loads	Q_c		1,0	–	1,0

1) 0,8 if 1 track only is loaded
0,7 if 2 tracks are simultaneously loaded
0,6 if 3 or more tracks are simultaneously loaded.
See A2.2.4(4).

2) When wind forces act simultaneously with traffic actions, the wind force $\psi_0 F_{Wk}$ should be taken as no greater than F_W^{**} (see EN 1991-1-4).

3) See EN 1991-1-5.

4) If deformation is being considered for Persistent and Transient design situations, ψ_2 should be taken equal to 1,00 for rail traffic actions. For seismic design situations, see Table A2.5.

5) Minimum coexistent favourable vertical load with individual components of rail traffic actions (e.g. centrifugal, traction or braking) is 0,5 LM71, etc.

NOTE 5 For specific design situations (e.g. calculation of bridge camber for aesthetics and drainage consideration, calculation of clearance, etc.) the requirements for the combinations of actions to be used may be defined for the individual project.

NOTE 6 For railway bridges, the infrequent value of variable actions is not relevant.

(2) [AC] For railway bridges «AC», a unique ψ value should be applied to one group of loads as defined in EN 1991-2, and taken as equal to the ψ value applicable to the leading component of the group.

ULS Load combinations:

- L1. Eq.610a
1,35*Seflweight
- L2. Eq.610b/1
1,25*Seflweight+1,45*TrafficLoad+1,50*0,75*Wind
- L3. Eq.610b/2
1,25*Seflweight+1,50*Wind+1,45*0,8*TrafficLoad

2.4 Materials

Steel Properties: Yield strength = 220 MPa
Ultimate tensile strength = 370 MPa
E = 205 000 MPa

Assumption is based on a UIC publication IRS 77802 "Assessment of Existing Steel Structures: Recommendations for Estimation of Remaining Fatigue Life".

Assessment of Existing Steel Structures, Remaining Fatigue Life

First edition 2008

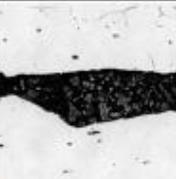
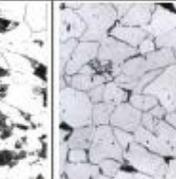
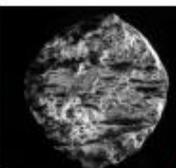
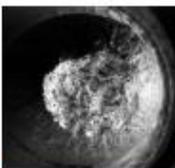
	Cast iron	Wrought steel Puddled steel	Mild steel (19th century)	Mild steel (20th century)
Sulphur-print (Baumann-print)	Content of sulphur is depending on coke quality	 Slag segregation lines containing phosphorus and sulphur	 Core segregation containing phosphorus and sulphur	 Low content of phosphorus and sulphur
Micro-structure ~1:400	 Cast iron with lamellar graphite	 Ferritic, Inhomogeneous grain size distribution, Oxide inclusions, Slag lines	 Ferritic-pearlitic, Increasing grain size from the edge to the core, Oxide and sulphide inclusions	 Homogenous small grain
Chemical analysis	C ≈ 2,0-4,0 % Mn ≈ 0,2-1,2 % Si ≈ 0,3-3,0 % S < ≈ 1,2 % P < ≈ 1,0 %	Very variable C < ≈ 0,08 % Mn < ≈ 0,4 % S < ≈ 0,04 % P < ≈ 0,6 %	Bessemer / Thomas steel C ≈ 0,02-0,1 % Mn ≈ 0,3-0,5 % S < ≈ 0,1 % P ≈ 0,04-0,07%(B) / -0,12%(T) Siemens-Martin steel C ≈ 0,05-0,15 % Mn ≈ 0,2-0,5 % S ≈ 0,02-0,15 % P ≈ 0,03-0,06 % Blast Process: N > ≈ 0,01%, Hearth Process: N < ≈ 0,01% Bessemer steel: Si > ≈ 0,08%, Thomas steel: Si < ≈ 0,08%	Low-alloyed steel (T, SM) C ≈ 0,1-0,2 % Mn ≈ 0,4-0,5 % Si ≈ 0,01 %
Tension test	Very brittle, almost no plasticity 	No local necking 	local necking 	Local necking and shear lips 
Tension strength	Old cast iron $R_m \approx 90-135^{1)} \text{ N/mm}^2$ $\epsilon^{2)} \approx 0 \%$	$R_e \approx 220-310 \text{ N/mm}^2$ $R_m \approx 280-400 \text{ N/mm}^2$ $\epsilon \approx 5-20 \%$	$R_e > \approx 220 \text{ N/mm}^2$ $R_m \approx 370-440 \text{ N/mm}^2$ $\epsilon > \approx 20 \%$	Low-alloyed steel $R_e \approx 240-280 \text{ N/mm}^2$ $R_m \approx 370-450 \text{ N/mm}^2$ $\epsilon \approx 15-25 \%$
Specimen after tension test	No local necking 		Local necking 	

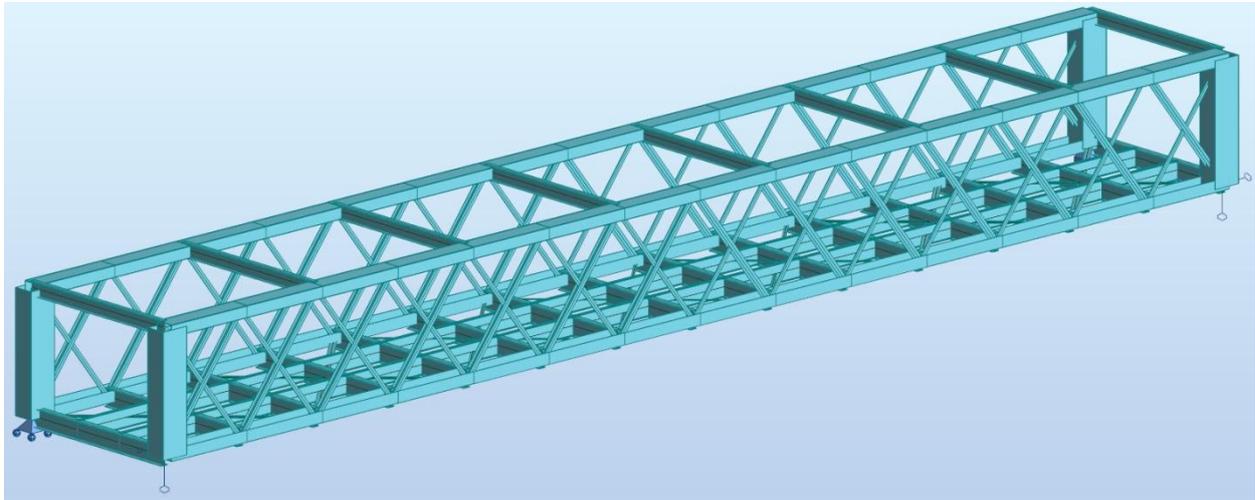
Table 3-2: Information on material characteristics of old iron and steels

¹⁾ Literature [Lit. 96] gives also higher values up to 260 N/mm²; ²⁾ elongation at rupture

Picture 29, steel material properties

3 RESULTS

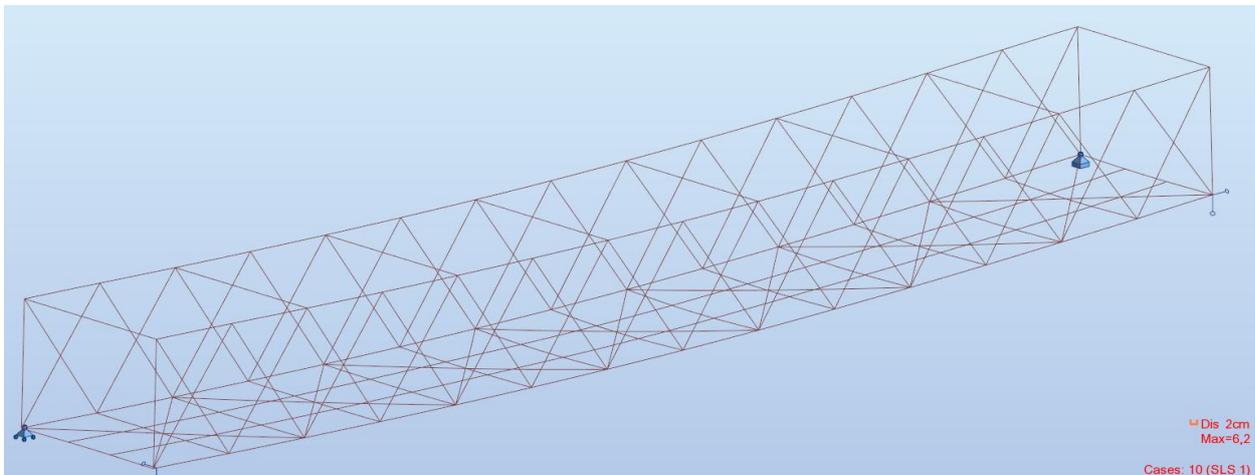
3.1 37 m span Lattice/Truss Bridge



Picture 30, View of FEM model

3.1.1 SLS results (Serviceability Limit State)

Total deflection of bridge is 6,2 cm = $L/600$ which is same as the limit.



Picture 31, Deflection

3.1.2 ULS results (Ultimate Limit State)

3.1.2.1 Lower main girders' utilization

The highest utilization ratio for the members is **0,75**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
156 Simple bar_1	Lower main girder	STEEL	12.15	25.85	0.75	5 L2.Eq610b
67 Simple bar_67	Lower main girder	STEEL	12.15	25.85	0.75	5 L2.Eq610b
148 Simple bar_1	Lower main girder	STEEL	12.15	25.85	0.71	5 L2.Eq610b
58 Simple bar_58	Lower main girder	STEEL	12.15	25.85	0.70	5 L2.Eq610b
66 Simple bar_66	Lower main girder	STEEL	12.15	25.85	0.67	5 L2.Eq610b
155 Simple bar_1	Lower main girder	STEEL	12.15	25.85	0.67	5 L2.Eq610b
139 Simple bar_1	Lower main girder	STEEL	12.15	25.85	0.64	5 L2.Eq610b
57 Simple bar_57	Lower main girder	STEEL	12.15	25.85	0.63	5 L2.Eq610b
49 Simple bar_49	Lower main girder	STEEL	12.15	25.85	0.63	5 L2.Eq610b
147 Simple bar_1	Lower main girder	STEEL	12.15	25.85	0.62	5 L2.Eq610b
130 Simple bar_1	Lower main girder	STEEL	12.14	25.90	0.61	5 L2.Eq610b
40 Simple bar_40	Lower main girder	STEEL	12.14	25.90	0.58	5 L2.Eq610b
48 Simple bar_48	Lower main girder	STEEL	12.15	25.85	0.57	5 L2.Eq610b
138 Simple bar_1	Lower main girder	STEEL	12.15	25.85	0.56	5 L2.Eq610b
39 Simple bar_39	Lower main girder	STEEL	12.14	25.90	0.55	5 L2.Eq610b
129 Simple bar_1	Lower main girder	STEEL	12.14	25.90	0.53	5 L2.Eq610b
8 Simple bar_8	Lower main girder	STEEL	12.14	25.90	0.49	8 L4.Eq610b/at supp
7 Simple bar_7	Lower main girder	STEEL	12.14	25.90	0.47	8 L4.Eq610b/at supp
98 Simple bar_98	Lower main girder	STEEL	12.14	25.90	0.47	5 L2.Eq610b
121 Simple bar_1	Lower main girder	STEEL	12.14	25.90	0.46	5 L2.Eq610b
112 Simple bar_1	Lower main girder	STEEL	12.14	25.90	0.45	5 L2.Eq610b
97 Simple bar_97	Lower main girder	STEEL	12.14	25.90	0.45	5 L2.Eq610b
31 Simple bar_31	Lower main girder	STEEL	12.14	25.90	0.44	5 L2.Eq610b
21 Simple bar_21	Lower main girder	STEEL	12.14	25.90	0.44	8 L4.Eq610b/at supp
30 Simple bar_30	Lower main girder	STEEL	12.14	25.90	0.42	5 L2.Eq610b
22 Simple bar_22	Lower main girder	STEEL	12.14	25.90	0.41	8 L4.Eq610b/at supp
120 Simple bar_1	Lower main girder	STEEL	12.14	25.90	0.40	5 L2.Eq610b
111 Simple bar_1	Lower main girder	STEEL	12.14	25.90	0.39	5 L2.Eq610b

Table 1, Utilization of lower main girder in order of utilization ratio

3.1.2.2 Upper main girders' utilization

The highest utilization ratio for the members is **0,84**.

The critical load combination was L2: 1,25*Seflweight+1,45*TrafficLoad+1,50*0,75*Wind, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
86 Simple bar_86	Upper main girder	STEEL	19.78	12.82	0.84	5 L2.Eq610b
175 Simple bar_1	Upper main girder	STEEL	19.78	12.82	0.84	5 L2.Eq610b
174 Simple bar_1	Upper main girder	STEEL	19.78	12.82	0.78	5 L2.Eq610b
85 Simple bar_85	Upper main girder	STEEL	19.78	12.82	0.78	5 L2.Eq610b
173 Simple bar_1	Upper main girder	STEEL	19.78	12.82	0.77	5 L2.Eq610b
84 Simple bar_84	Upper main girder	STEEL	19.78	12.82	0.77	5 L2.Eq610b
172 Simple bar_1	Upper main girder	STEEL	19.78	12.82	0.72	5 L2.Eq610b
83 Simple bar_83	Upper main girder	STEEL	19.78	12.82	0.72	5 L2.Eq610b
171 Simple bar_1	Upper main girder	STEEL	19.78	12.82	0.69	5 L2.Eq610b
82 Simple bar_82	Upper main girder	STEEL	19.78	12.82	0.69	5 L2.Eq610b
170 Simple bar_1	Upper main girder	STEEL	19.78	12.82	0.64	5 L2.Eq610b
81 Simple bar_81	Upper main girder	STEEL	19.78	12.82	0.64	5 L2.Eq610b
169 Simple bar_1	Upper main girder	STEEL	19.73	12.98	0.55	5 L2.Eq610b
80 Simple bar_80	Upper main girder	STEEL	19.73	12.98	0.55	5 L2.Eq610b
168 Simple bar_1	Upper main girder	STEEL	19.73	12.98	0.51	5 L2.Eq610b
79 Simple bar_79	Upper main girder	STEEL	19.73	12.98	0.51	5 L2.Eq610b
167 Simple bar_1	Upper main girder	STEEL	19.73	12.98	0.45	5 L2.Eq610b
78 Simple bar_78	Upper main girder	STEEL	19.73	12.98	0.44	5 L2.Eq610b
166 Simple bar_1	Upper main girder	STEEL	19.73	12.98	0.41	5 L2.Eq610b
77 Simple bar_77	Upper main girder	STEEL	19.73	12.98	0.41	5 L2.Eq610b
100 Simple bar_1	Upper main girder	STEEL	19.73	12.98	0.37	5 L2.Eq610b
10 Simple bar_10	Upper main girder	STEEL	19.73	12.98	0.37	5 L2.Eq610b
9 Simple bar_9	Upper main girder	STEEL	19.73	12.98	0.34	5 L2.Eq610b
99 Simple bar_99	Upper main girder	STEEL	19.73	12.98	0.34	5 L2.Eq610b
76 Simple bar_76	Upper main girder	STEEL	19.73	12.98	0.33	8 L4.Eq610b/at supp
165 Simple bar_1	Upper main girder	STEEL	19.73	12.98	0.32	5 L2.Eq610b
75 Simple bar_75	Upper main girder	STEEL	19.73	12.98	0.30	8 L4.Eq610b/at supp
164 Simple bar_1	Upper main girder	STEEL	19.73	12.98	0.29	5 L2.Eq610b

Table 2, Utilization of upper main girder in order of utilization ratio

3.1.2.3 Diagonals' utilization

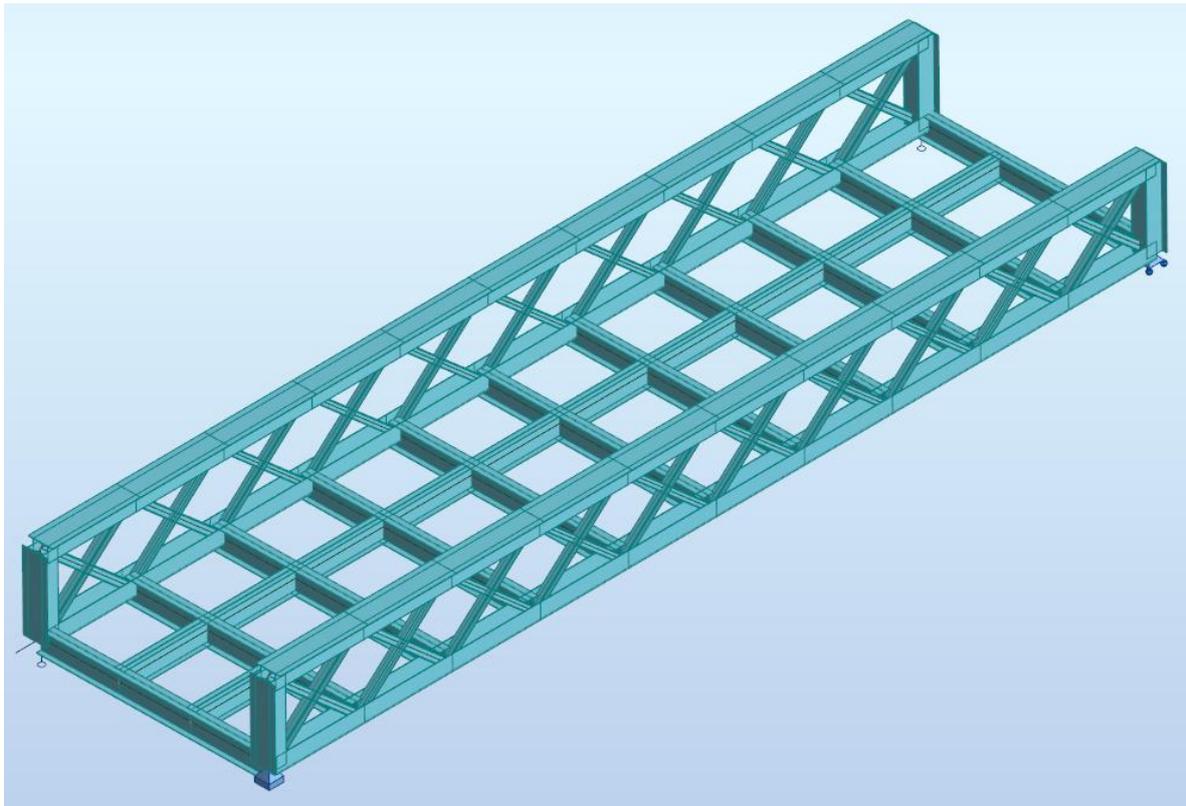
The highest utilization ratio for the members is **0,81**.

The critical load combination was L2: 1,25*Seflweight+1,45*TrafficLoad+1,50*0,75*Wind, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
16 Simple bar3_1	Diagonals	STEEL	6.85	11.92	0.81	5 L2.Eq610b
106 Simple bar3	Diagonals	STEEL	6.85	11.92	0.81	5 L2.Eq610b
105 Simple bar3	Diagonals	STEEL	6.85	11.92	0.75	5 L2.Eq610b
15 Simple bar3_1	Diagonals	STEEL	6.85	11.92	0.75	5 L2.Eq610b
116 Simple bar3	Diagonals	STEEL	6.85	11.92	0.59	5 L2.Eq610b
26 Simple bar3_2	Diagonals	STEEL	6.85	11.92	0.59	5 L2.Eq610b
25 Simple bar3_2	Diagonals	STEEL	6.85	11.92	0.55	5 L2.Eq610b
115 Simple bar3	Diagonals	STEEL	6.85	11.92	0.55	5 L2.Eq610b
125 Simple bar3	Diagonals	STEEL	6.85	11.92	0.52	5 L2.Eq610b
35 Simple bar3_3	Diagonals	STEEL	6.85	11.92	0.52	5 L2.Eq610b
124 Simple bar3	Diagonals	STEEL	6.85	11.92	0.49	5 L2.Eq610b
34 Simple bar3_3	Diagonals	STEEL	6.85	11.92	0.48	5 L2.Eq610b
133 Simple bar3	Diagonals	STEEL	6.85	11.92	0.39	5 L2.Eq610b
44 Simple bar3_4	Diagonals	STEEL	7.03	11.83	0.36	5 L2.Eq610b
134 Simple bar3	Diagonals	STEEL	7.03	11.83	0.36	5 L2.Eq610b
43 Simple bar3_4	Diagonals	STEEL	7.03	11.83	0.34	5 L2.Eq610b
143 Simple bar3	Diagonals	STEEL	7.03	11.83	0.27	5 L2.Eq610b
53 Simple bar3_5	Diagonals	STEEL	7.03	11.83	0.27	5 L2.Eq610b
142 Simple bar3	Diagonals	STEEL	7.03	11.83	0.26	5 L2.Eq610b
52 Simple bar3_5	Diagonals	STEEL	7.03	11.83	0.25	5 L2.Eq610b
62 Simple bar3_6	Diagonals	STEEL	7.03	11.83	0.17	5 L2.Eq610b
152 Simple bar3	Diagonals	STEEL	7.03	11.83	0.17	5 L2.Eq610b
61 Simple bar3_6	Diagonals	STEEL	7.03	11.83	0.16	5 L2.Eq610b
151 Simple bar3	Diagonals	STEEL	7.03	11.83	0.16	5 L2.Eq610b
159 Simple bar3	Diagonals	STEEL	7.03	11.83	0.01	8 L4.Eq610b/at supp
160 Simple bar3	Diagonals	STEEL	7.03	11.83	0.01	8 L4.Eq610b/at supp

Table 3, Utilization of diagonals in order of utilization ratio

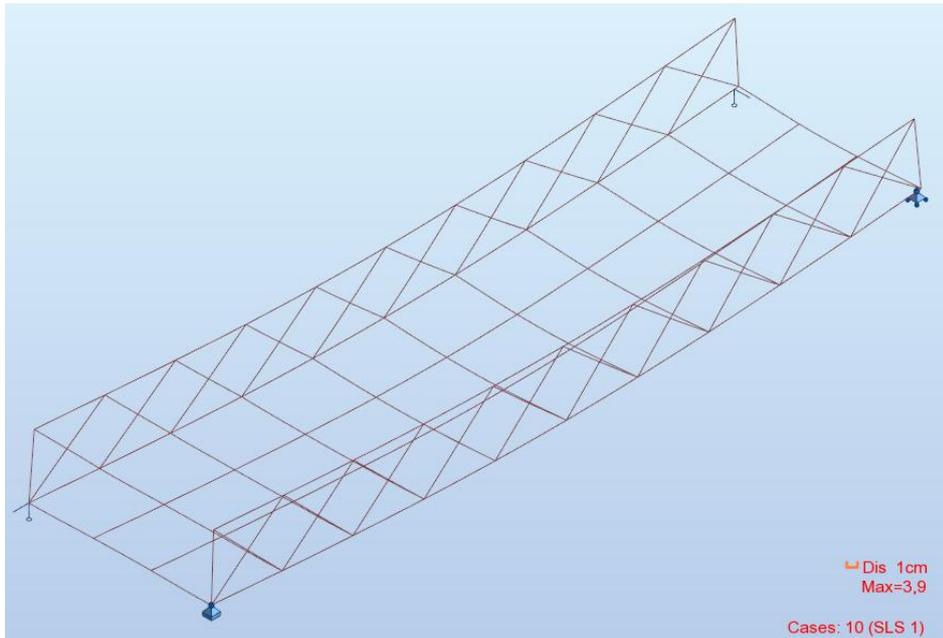
3.2 18,67 m span truss bridge



Picture 34, View of FEM model

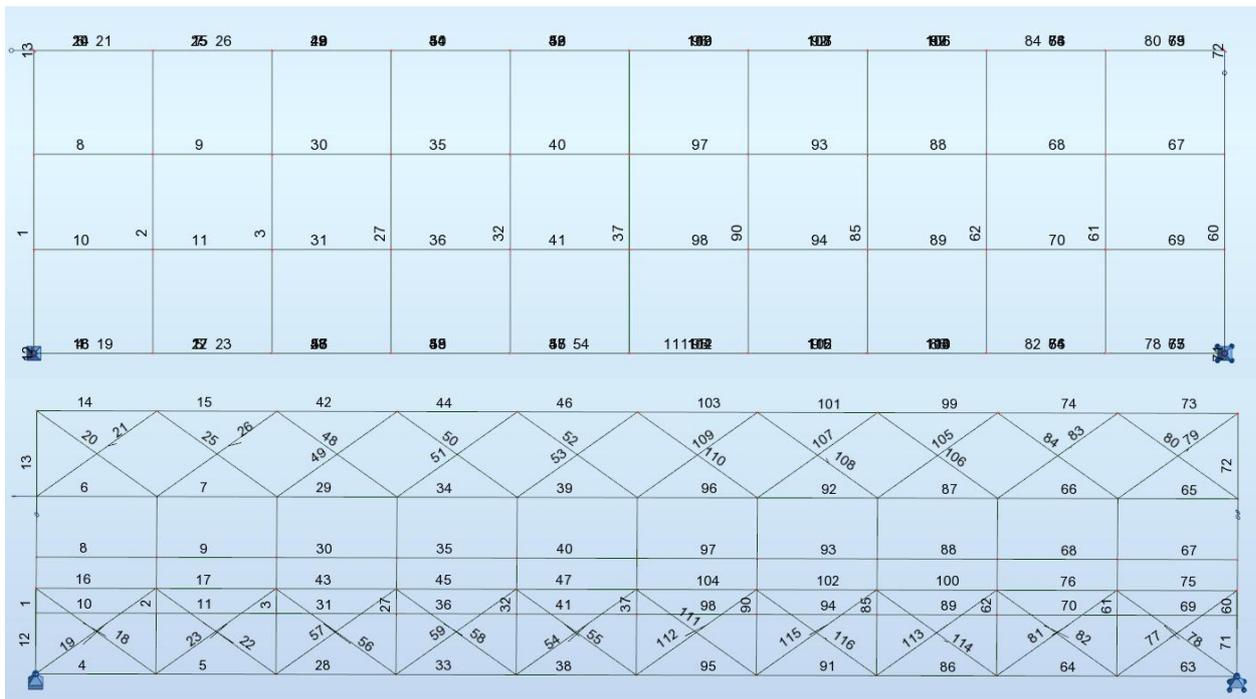
3.2.1 SLS results (Serviceability Limit State)

Total deflection of bridge is 3,9 cm = L/487



Picture 35, Deflection

3.2.2 ULS results (Ultimate Limit State)



Picture 36, member numbers for profiles that will be utilized – top view, side view

After analysis, an utilization ratio may be calculated for each member of the bridge truss.

3.2.2.1 Cross beams' utilization

The highest utilization ratio for the members is **0,88**.

The critical load combination was L4: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at support.

Member	Section	Material	Lay	Laz	Ratio	Case
1 Simple bar_1	Cross beam	STEEL	28.41	124.22	0.88	8 L4.Eq610b/at supp
3 Simple bar_3	Cross beam	STEEL	28.41	124.22	0.85	8 L4.Eq610b/at supp
2 Simple bar_2	Cross beam	STEEL	28.41	124.22	0.83	8 L4.Eq610b/at supp
60 Simple bar_60	Cross beam	STEEL	28.41	124.22	0.69	5 L2.Eq610b
32 Simple bar_32	Cross beam	STEEL	28.41	124.22	0.69	5 L2.Eq610b
90 Simple bar_90	Cross beam	STEEL	28.41	124.22	0.67	5 L2.Eq610b
61 Simple bar_61	Cross beam	STEEL	28.41	124.22	0.67	6 L3.Eq610b
62 Simple bar_62	Cross beam	STEEL	28.41	124.22	0.66	5 L2.Eq610b
27 Simple bar_27	Cross beam	STEEL	28.41	124.22	0.65	8 L4.Eq610b/at supp
37 Simple bar_37	Cross beam	STEEL	28.41	124.22	0.64	5 L2.Eq610b
85 Simple bar_85	Cross beam	STEEL	28.41	124.22	0.63	5 L2.Eq610b

Table 4, Utilization of cross beams in order of utilization ratio

3.2.2.2 Longitudinal girders' utilization

The highest utilization ratio for the members is **0,94**.

The critical load combination was L3: $1,25 \cdot \text{Selfweight} + 1,50 \cdot \text{Wind} + 1,45 \cdot 0,8 \cdot \text{TrafficLoad}$, and the traffic load's point loads were placed at midspan.

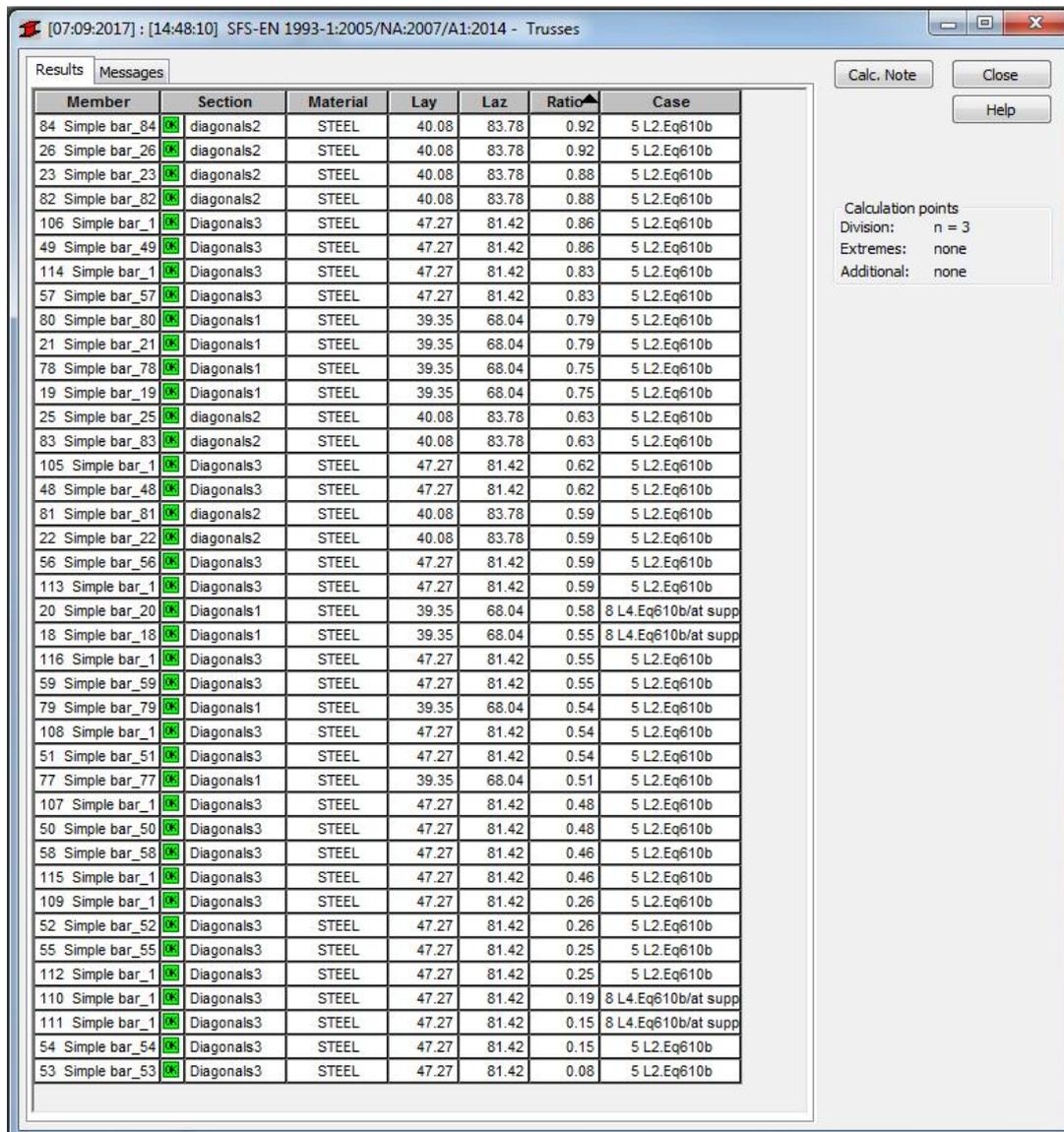
Member	Section	Material	Lay	Laz	Ratio	Case
10 Simple bar_10	Longitudinal girder	STEEL	11.43	57.03	0.94	6 L3.Eq610b
69 Simple bar_69	Longitudinal girder	STEEL	11.43	57.03	0.87	6 L3.Eq610b
11 Simple bar_11	Longitudinal girder	STEEL	11.43	57.03	0.82	6 L3.Eq610b
70 Simple bar_70	Longitudinal girder	STEEL	11.43	57.03	0.76	6 L3.Eq610b
31 Simple bar_31	Longitudinal girder	STEEL	11.43	57.03	0.66	6 L3.Eq610b
36 Simple bar_36	Longitudinal girder	STEEL	11.43	57.03	0.64	5 L2.Eq610b
94 Simple bar_94	Longitudinal girder	STEEL	11.43	57.03	0.62	5 L2.Eq610b
40 Simple bar_40	Longitudinal girder	STEEL	11.43	57.03	0.61	5 L2.Eq610b
97 Simple bar_97	Longitudinal girder	STEEL	11.43	57.03	0.60	5 L2.Eq610b
89 Simple bar_89	Longitudinal girder	STEEL	11.43	57.03	0.60	6 L3.Eq610b
98 Simple bar_98	Longitudinal girder	STEEL	11.43	57.03	0.59	5 L2.Eq610b
41 Simple bar_41	Longitudinal girder	STEEL	11.43	57.03	0.59	5 L2.Eq610b
93 Simple bar_93	Longitudinal girder	STEEL	11.43	57.03	0.51	5 L2.Eq610b
35 Simple bar_35	Longitudinal girder	STEEL	11.43	57.03	0.51	5 L2.Eq610b
30 Simple bar_30	Longitudinal girder	STEEL	11.43	57.03	0.47	8 L4.Eq610b/at supp
9 Simple bar_9	Longitudinal girder	STEEL	11.43	57.03	0.41	8 L4.Eq610b/at supp
8 Simple bar_8	Longitudinal girder	STEEL	11.43	57.03	0.35	2 Wind
67 Simple bar_67	Longitudinal girder	STEEL	11.43	57.03	0.30	2 Wind
68 Simple bar_68	Longitudinal girder	STEEL	11.43	57.03	0.27	3 LM71-22,5
88 Simple bar_88	Longitudinal girder	STEEL	11.43	57.03	0.24	8 L4.Eq610b/at supp

Table 5, Utilization of longitudinal girders in order of utilization ratio

3.2.2.3 Trusses/diagonals' utilization

The highest utilization ratio for the members is **0,92**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.



Member	Section	Material	Lay	Laz	Ratio	Case
84 Simple bar_84	diagonals2	STEEL	40.08	83.78	0.92	5 L2.Eq610b
26 Simple bar_26	diagonals2	STEEL	40.08	83.78	0.92	5 L2.Eq610b
23 Simple bar_23	diagonals2	STEEL	40.08	83.78	0.88	5 L2.Eq610b
82 Simple bar_82	diagonals2	STEEL	40.08	83.78	0.88	5 L2.Eq610b
106 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.86	5 L2.Eq610b
49 Simple bar_49	Diagonals3	STEEL	47.27	81.42	0.86	5 L2.Eq610b
114 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.83	5 L2.Eq610b
57 Simple bar_57	Diagonals3	STEEL	47.27	81.42	0.83	5 L2.Eq610b
80 Simple bar_80	Diagonals1	STEEL	39.35	68.04	0.79	5 L2.Eq610b
21 Simple bar_21	Diagonals1	STEEL	39.35	68.04	0.79	5 L2.Eq610b
78 Simple bar_78	Diagonals1	STEEL	39.35	68.04	0.75	5 L2.Eq610b
19 Simple bar_19	Diagonals1	STEEL	39.35	68.04	0.75	5 L2.Eq610b
25 Simple bar_25	diagonals2	STEEL	40.08	83.78	0.63	5 L2.Eq610b
83 Simple bar_83	diagonals2	STEEL	40.08	83.78	0.63	5 L2.Eq610b
105 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.62	5 L2.Eq610b
48 Simple bar_48	Diagonals3	STEEL	47.27	81.42	0.62	5 L2.Eq610b
81 Simple bar_81	diagonals2	STEEL	40.08	83.78	0.59	5 L2.Eq610b
22 Simple bar_22	diagonals2	STEEL	40.08	83.78	0.59	5 L2.Eq610b
56 Simple bar_56	Diagonals3	STEEL	47.27	81.42	0.59	5 L2.Eq610b
113 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.59	5 L2.Eq610b
20 Simple bar_20	Diagonals1	STEEL	39.35	68.04	0.58	8 L4.Eq610b/at supp
18 Simple bar_18	Diagonals1	STEEL	39.35	68.04	0.55	8 L4.Eq610b/at supp
116 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.55	5 L2.Eq610b
59 Simple bar_59	Diagonals3	STEEL	47.27	81.42	0.55	5 L2.Eq610b
79 Simple bar_79	Diagonals1	STEEL	39.35	68.04	0.54	5 L2.Eq610b
108 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.54	5 L2.Eq610b
51 Simple bar_51	Diagonals3	STEEL	47.27	81.42	0.54	5 L2.Eq610b
77 Simple bar_77	Diagonals1	STEEL	39.35	68.04	0.51	5 L2.Eq610b
107 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.48	5 L2.Eq610b
50 Simple bar_50	Diagonals3	STEEL	47.27	81.42	0.48	5 L2.Eq610b
58 Simple bar_58	Diagonals3	STEEL	47.27	81.42	0.46	5 L2.Eq610b
115 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.46	5 L2.Eq610b
109 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.26	5 L2.Eq610b
52 Simple bar_52	Diagonals3	STEEL	47.27	81.42	0.26	5 L2.Eq610b
55 Simple bar_55	Diagonals3	STEEL	47.27	81.42	0.25	5 L2.Eq610b
112 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.25	5 L2.Eq610b
110 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.19	8 L4.Eq610b/at supp
111 Simple bar_1	Diagonals3	STEEL	47.27	81.42	0.15	8 L4.Eq610b/at supp
54 Simple bar_54	Diagonals3	STEEL	47.27	81.42	0.15	5 L2.Eq610b
53 Simple bar_53	Diagonals3	STEEL	47.27	81.42	0.08	5 L2.Eq610b

Table 6, Utilization of trusses in order of utilization ratio

3.2.2.4 Lower main girders' utilization

The highest utilization ratio for the members is **0,77**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
96 Simple bar_96	Lower main gi	STEEL	14.64	18.05	0.77	5 L2.Eq610b
39 Simple bar_39	Lower main gi	STEEL	14.64	18.05	0.77	5 L2.Eq610b
38 Simple bar_38	Lower main gi	STEEL	14.64	18.05	0.70	5 L2.Eq610b
95 Simple bar_95	Lower main gi	STEEL	14.64	18.05	0.70	5 L2.Eq610b
92 Simple bar_92	Lower main gi	STEEL	14.64	18.05	0.69	5 L2.Eq610b
34 Simple bar_34	Lower main gi	STEEL	14.64	18.05	0.69	5 L2.Eq610b
33 Simple bar_33	Lower main gi	STEEL	14.64	18.05	0.63	5 L2.Eq610b
91 Simple bar_91	Lower main gi	STEEL	14.64	18.05	0.63	5 L2.Eq610b
87 Simple bar_87	Lower main gi	STEEL	14.64	18.05	0.56	5 L2.Eq610b
29 Simple bar_29	Lower main gi	STEEL	14.64	18.05	0.56	5 L2.Eq610b
28 Simple bar_28	Lower main gi	STEEL	14.64	18.05	0.51	5 L2.Eq610b
86 Simple bar_86	Lower main gi	STEEL	14.64	18.05	0.51	5 L2.Eq610b
66 Simple bar_66	Lower main gi	STEEL	14.64	18.05	0.36	5 L2.Eq610b
7 Simple bar_7	Lower main gi	STEEL	14.64	18.05	0.36	5 L2.Eq610b
4 Simple bar_4	Lower main gi	STEEL	14.64	18.05	0.33	8 L4.Eq610b/at supp
5 Simple bar_5	Lower main gi	STEEL	14.64	18.05	0.33	5 L2.Eq610b
64 Simple bar_64	Lower main gi	STEEL	14.64	18.05	0.32	5 L2.Eq610b
63 Simple bar_63	Lower main gi	STEEL	14.64	18.05	0.30	5 L2.Eq610b
6 Simple bar_6	Lower main gi	STEEL	14.64	18.05	0.28	8 L4.Eq610b/at supp
65 Simple bar_65	Lower main gi	STEEL	14.64	18.05	0.25	5 L2.Eq610b

Table 7, Utilization of lower main girder in order of utilization ratio

3.2.2.5 Upper main girders' utilization

The highest utilization ratio for the members is **0,92**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
103 Simple bar_1	Upper main gir	STEEL	15.66	12.86	0.92	5 L2.Eq610b
46 Simple bar_46	Upper main gir	STEEL	15.66	12.86	0.92	5 L2.Eq610b
104 Simple bar_1	Upper main gir	STEEL	15.66	12.86	0.91	5 L2.Eq610b
47 Simple bar_47	Upper main gir	STEEL	15.66	12.86	0.91	5 L2.Eq610b
101 Simple bar_1	Upper main gir	STEEL	15.66	12.86	0.84	5 L2.Eq610b
44 Simple bar_44	Upper main gir	STEEL	15.66	12.86	0.84	5 L2.Eq610b
102 Simple bar_1	Upper main gir	STEEL	15.66	12.86	0.83	5 L2.Eq610b
45 Simple bar_45	Upper main gir	STEEL	15.66	12.86	0.83	5 L2.Eq610b
99 Simple bar_99	Upper main gir	STEEL	15.66	12.86	0.69	5 L2.Eq610b
42 Simple bar_42	Upper main gir	STEEL	15.66	12.86	0.69	5 L2.Eq610b
100 Simple bar_1	Upper main gir	STEEL	15.66	12.86	0.67	5 L2.Eq610b
43 Simple bar_43	Upper main gir	STEEL	15.66	12.86	0.67	5 L2.Eq610b
15 Simple bar_15	Upper main gir	STEEL	15.66	12.86	0.47	8 L4.Eq610b/at supp
74 Simple bar_74	Upper main gir	STEEL	15.66	12.86	0.46	5 L2.Eq610b
17 Simple bar_17	Upper main gir	STEEL	15.66	12.86	0.45	8 L4.Eq610b/at supp
76 Simple bar_76	Upper main gir	STEEL	15.66	12.86	0.43	5 L2.Eq610b
73 Simple bar_73	Upper main gir	STEEL	15.66	12.86	0.37	5 L2.Eq610b
14 Simple bar_14	Upper main gir	STEEL	15.66	12.86	0.37	5 L2.Eq610b
16 Simple bar_16	Upper main gir	STEEL	15.66	12.86	0.36	8 L4.Eq610b/at supp
75 Simple bar_75	Upper main gir	STEEL	15.66	12.86	0.35	5 L2.Eq610b

Table 8, Utilization of upper main girder in order of utilization ratio

3.2.2.6 End columns' utilization

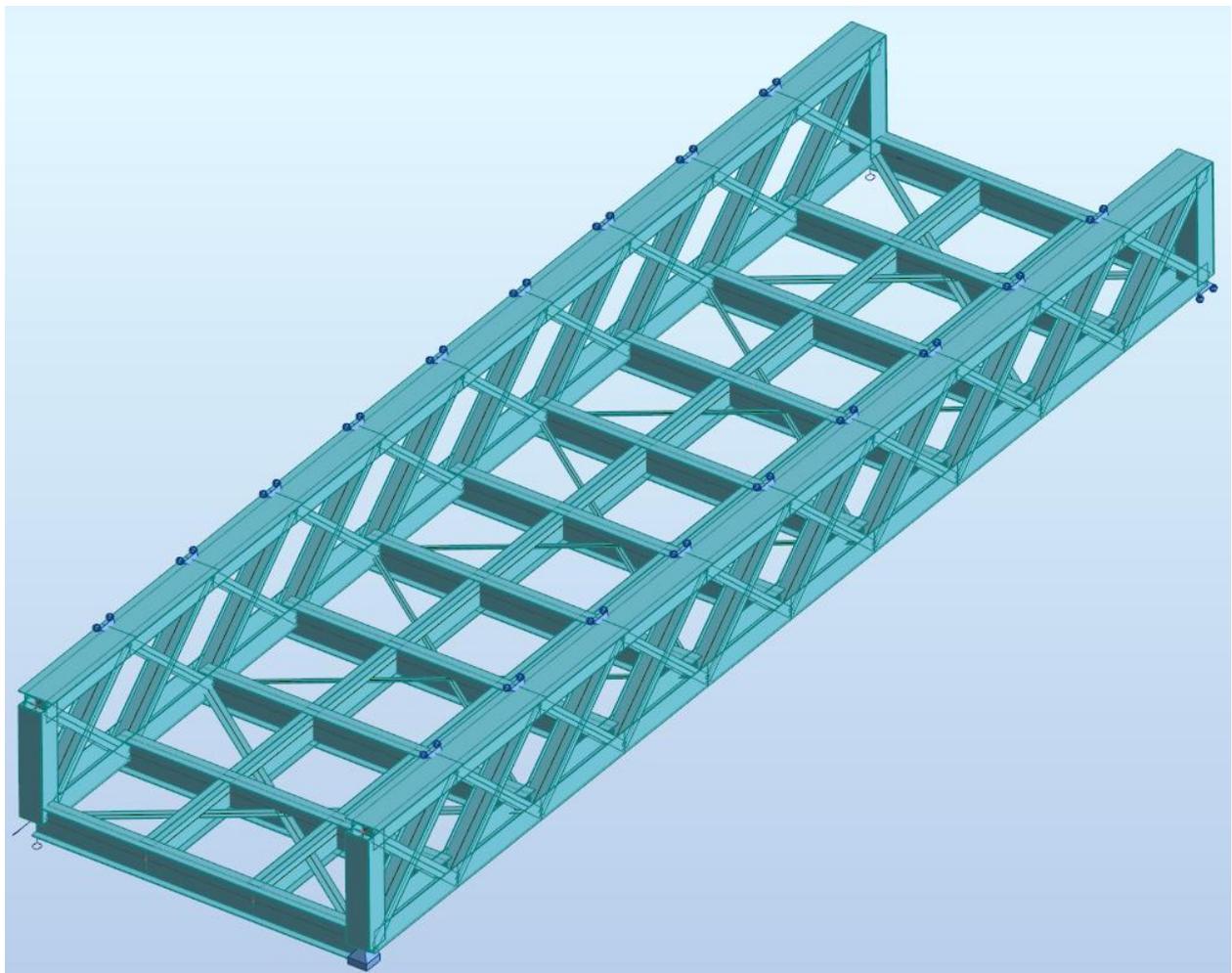
The highest utilization ratio for the members is **0,34**.

The critical load combination was $L4: 1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at support.

Member	Section	Material	Lay	Laz	Ratio	Case
13 Simple bar_13	End Frame	STEEL	13.26	11.36	0.34	8 L4.Eq610b/at supp
72 Simple bar_72	End Frame	STEEL	13.26	11.36	0.33	5 L2.Eq610b
12 Simple bar_12	End Frame	STEEL	13.26	11.36	0.33	8 L4.Eq610b/at supp
71 Simple bar_71	End Frame	STEEL	13.26	11.36	0.31	5 L2.Eq610b

Table 9, Utilization of end frame in order of utilization ratio

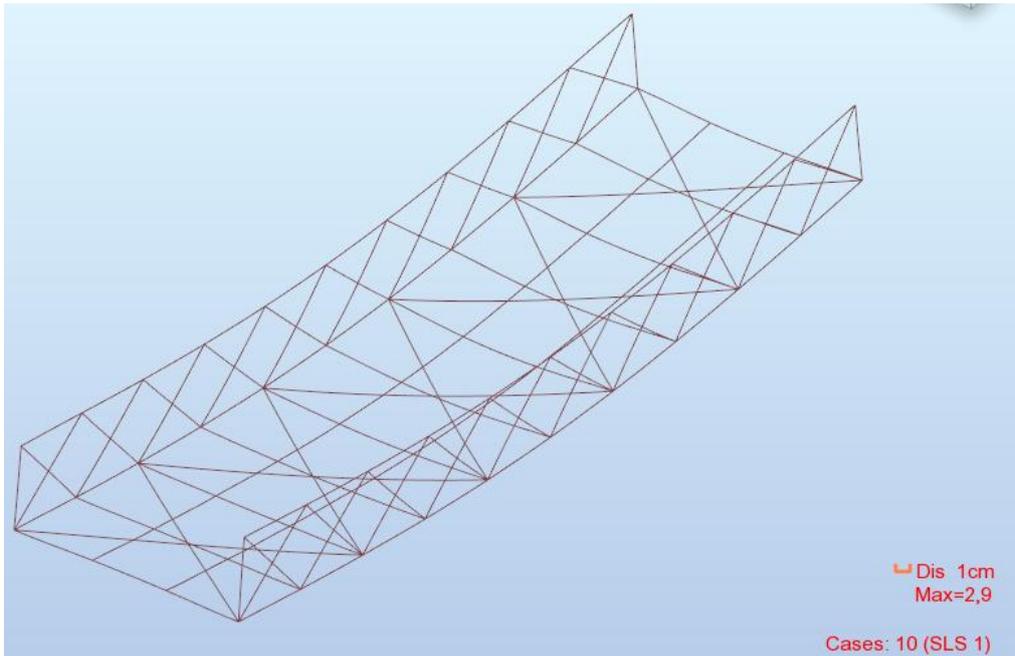
3.3 17 m span truss bridge



Picture 37, View of FEM model

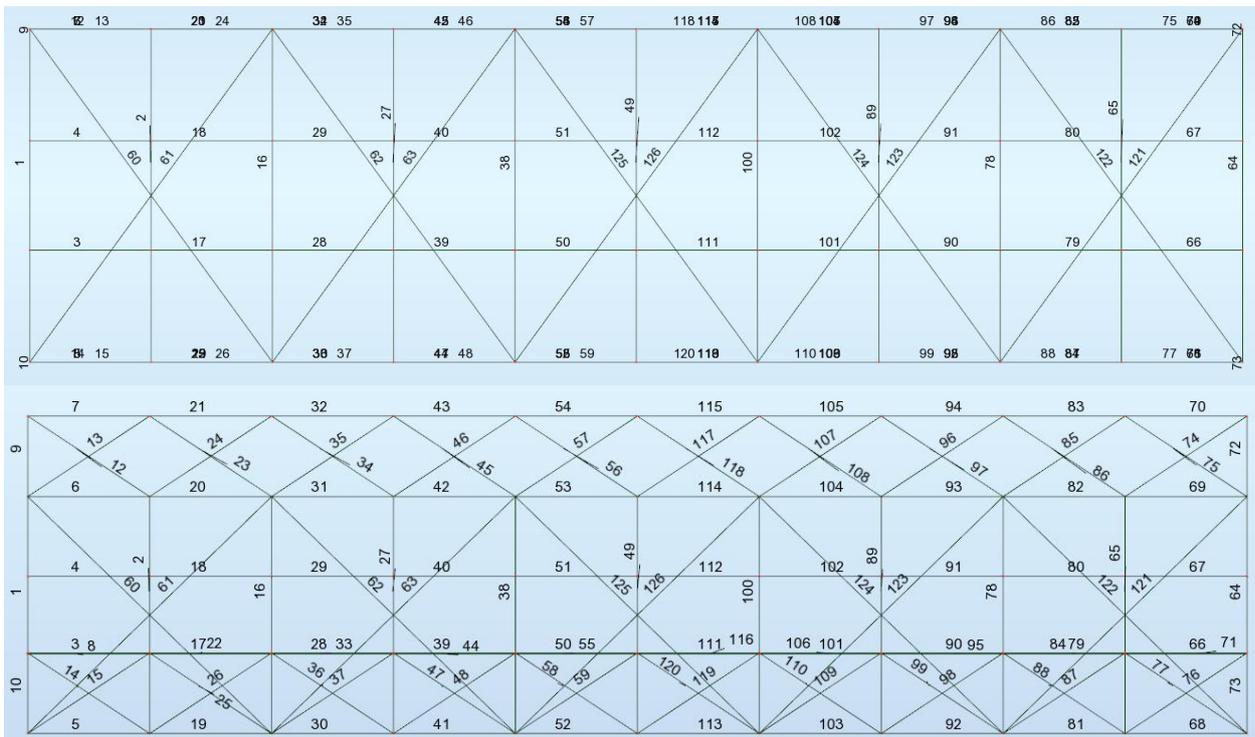
3.3.1 SLS results (Serviceability Limit State)

Total deflection of bridge is 2,9 cm = $L/586$



Picture 38, Deflection

3.3.2 ULS results (Ultimate Limit State)



Picture 39, member numbers for profiles that will be utilized – top view, side view

3.3.2.1 Cross beams' utilization

The highest utilization ratio for the members is **0,90**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
49 Beam_49	Cross beam	STEEL	28.16	122.59	0.90	5 L2.Eq610b
16 Beam_16	Cross beam	STEEL	28.16	122.59	0.88	8 L4.Eq610b/at supp
100 Beam_100	Cross beam	STEEL	28.16	122.59	0.87	5 L2.Eq610b
38 Beam_38	Cross beam	STEEL	28.16	122.59	0.85	5 L2.Eq610b
2 Beam_2	Cross beam	STEEL	28.16	122.59	0.84	8 L4.Eq610b/at supp
1 Column_1	Cross beam	STEEL	28.16	122.59	0.79	8 L4.Eq610b/at supp
27 Beam_27	Cross beam	STEEL	28.16	122.59	0.75	8 L4.Eq610b/at supp
89 Beam_89	Cross beam	STEEL	28.16	122.59	0.69	5 L2.Eq610b
78 Beam_78	Cross beam	STEEL	28.16	122.59	0.65	5 L2.Eq610b
64 Beam_64	Cross beam	STEEL	28.16	122.59	0.45	5 L2.Eq610b
65 Beam_65	Cross beam	STEEL	28.16	122.59	0.44	8 L4.Eq610b/at supp

Table 10, Utilization of cross beams in order of utilization ratio

3.3.2.2 Longitudinal girders' utilization

The highest utilization ratio for the members is **0,54**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
112 Simple bar_1	Longitudinal gi	STEEL	10.75	52.45	0.54	5 L2.Eq610b
111 Simple bar_1	Longitudinal gi	STEEL	10.75	52.45	0.52	5 L2.Eq610b
51 Simple bar_51	Longitudinal gi	STEEL	10.75	52.45	0.52	5 L2.Eq610b
102 Simple bar_1	Longitudinal gi	STEEL	10.75	52.45	0.51	5 L2.Eq610b
17 Simple bar_17	Longitudinal gi	STEEL	10.75	52.45	0.50	8 L4.Eq610b/at supp
3 Simple bar_3	Longitudinal gi	STEEL	10.75	52.45	0.50	5 L2.Eq610b
50 Simple bar_50	Longitudinal gi	STEEL	10.75	52.45	0.50	5 L2.Eq610b
101 Simple bar_1	Longitudinal gi	STEEL	10.75	52.45	0.50	5 L2.Eq610b
28 Simple bar_28	Longitudinal gi	STEEL	10.75	52.45	0.50	8 L4.Eq610b/at supp
40 Simple bar_40	Longitudinal gi	STEEL	10.75	52.45	0.49	5 L2.Eq610b
39 Simple bar_39	Longitudinal gi	STEEL	10.75	52.45	0.49	5 L2.Eq610b
66 Simple bar_66	Longitudinal gi	STEEL	10.75	52.45	0.49	5 L2.Eq610b
29 Simple bar_29	Longitudinal gi	STEEL	10.75	52.45	0.48	8 L4.Eq610b/at supp
18 Simple bar_18	Longitudinal gi	STEEL	10.75	52.45	0.48	8 L4.Eq610b/at supp
4 Simple bar_4	Longitudinal gi	STEEL	10.75	52.45	0.45	8 L4.Eq610b/at supp
67 Simple bar_67	Longitudinal gi	STEEL	10.75	52.45	0.45	5 L2.Eq610b
79 Simple bar_79	Longitudinal gi	STEEL	10.75	52.45	0.44	5 L2.Eq610b
80 Simple bar_80	Longitudinal gi	STEEL	10.75	52.45	0.43	5 L2.Eq610b
90 Simple bar_90	Longitudinal gi	STEEL	10.75	52.45	0.33	5 L2.Eq610b
91 Simple bar_91	Longitudinal gi	STEEL	10.75	52.45	0.31	8 L4.Eq610b/at supp

Table 11, Utilization of longitudinal girders in order of utilization ratio

3.3.2.3 Trusses/diagonals' utilization

The highest utilization ratio for the members is **0,93**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

SFS-EN 1993-1:2005/NA:2007/A1:2014 - Member Verification (ULS) 12to15 23to26 34to37 45to48 56to59 74to77...

Member	Section	Material	Lay	Laz	Ratio	Case
24 Simple bar_24	Diagonals2	STEEL	18.91	86.67	0.93	5 L2.Eq610b
86 Simple bar_86	Diagonals2	STEEL	18.91	86.67	0.93	5 L2.Eq610b
88 Simple bar_88	Diagonals2	STEEL	18.91	86.67	0.86	5 L2.Eq610b
13 Simple bar_13	Diagonals1	STEEL	17.86	65.66	0.85	8 L4.Eq610b/at supp
26 Simple bar_26	Diagonals2	STEEL	18.91	86.67	0.85	5 L2.Eq610b
15 Simple bar_15	Diagonals1	STEEL	17.86	65.66	0.82	8 L4.Eq610b/at supp
99 Simple bar_99	Diagonals3	STEEL	18.19	81.04	0.79	5 L2.Eq610b
37 Simple bar_37	Diagonals3	STEEL	18.19	81.04	0.78	5 L2.Eq610b
35 Simple bar_35	Diagonals3	STEEL	18.19	81.04	0.76	5 L2.Eq610b
75 Simple bar_75	Diagonals1	STEEL	17.86	65.66	0.76	5 L2.Eq610b
97 Simple bar_97	Diagonals3	STEEL	18.19	81.04	0.76	5 L2.Eq610b
77 Simple bar_77	Diagonals1	STEEL	17.86	65.66	0.75	5 L2.Eq610b
110 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.64	5 L2.Eq610b
48 Simple bar_48	Diagonals3	STEEL	18.19	81.04	0.64	5 L2.Eq610b
25 Simple bar_25	Diagonals2	STEEL	18.91	86.67	0.59	8 L4.Eq610b/at supp
46 Simple bar_46	Diagonals3	STEEL	18.19	81.04	0.59	5 L2.Eq610b
108 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.59	5 L2.Eq610b
23 Simple bar_23	Diagonals2	STEEL	18.91	86.67	0.54	8 L4.Eq610b/at supp
12 Simple bar_12	Diagonals1	STEEL	17.86	65.66	0.50	8 L4.Eq610b/at supp
85 Simple bar_85	Diagonals2	STEEL	18.91	86.67	0.49	5 L2.Eq610b
14 Simple bar_14	Diagonals1	STEEL	17.86	65.66	0.48	8 L4.Eq610b/at supp
87 Simple bar_87	Diagonals2	STEEL	18.91	86.67	0.47	5 L2.Eq610b
74 Simple bar_74	Diagonals1	STEEL	17.86	65.66	0.47	5 L2.Eq610b
120 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.45	5 L2.Eq610b
76 Simple bar_76	Diagonals1	STEEL	17.86	65.66	0.45	5 L2.Eq610b
59 Simple bar_59	Diagonals3	STEEL	18.19	81.04	0.44	5 L2.Eq610b
96 Simple bar_96	Diagonals3	STEEL	18.19	81.04	0.43	5 L2.Eq610b
34 Simple bar_34	Diagonals3	STEEL	18.19	81.04	0.42	5 L2.Eq610b
98 Simple bar_98	Diagonals3	STEEL	18.19	81.04	0.41	5 L2.Eq610b
36 Simple bar_36	Diagonals3	STEEL	18.19	81.04	0.41	5 L2.Eq610b
118 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.38	5 L2.Eq610b
57 Simple bar_57	Diagonals3	STEEL	18.19	81.04	0.37	5 L2.Eq610b
109 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.35	5 L2.Eq610b
47 Simple bar_47	Diagonals3	STEEL	18.19	81.04	0.33	5 L2.Eq610b
107 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.32	5 L2.Eq610b
45 Simple bar_45	Diagonals3	STEEL	18.19	81.04	0.32	5 L2.Eq610b
119 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.25	5 L2.Eq610b
58 Simple bar_58	Diagonals3	STEEL	18.19	81.04	0.25	5 L2.Eq610b
56 Simple bar_56	Diagonals3	STEEL	18.19	81.04	0.17	5 L2.Eq610b
117 Simple bar_1	Diagonals3	STEEL	18.19	81.04	0.17	5 L2.Eq610b

Calc. Note Close
 Help
 Ratio
 Analysis Map
 Calculation points
 Division: n = 3
 Extremes: none
 Additional: none

Table 12, Utilization of trusses in order of utilization ratio

3.3.2.4 Lower main girders' utilization

The highest utilization ratio for the members is **0,66**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

Member	Section	Material	Lay	Laz	Ratio	Case
114 Simple bar_1	Lower main gi	STEEL	13.54	16.70	0.66	5 L2.Eq610b
53 Simple bar_53	Lower main gi	STEEL	13.54	16.70	0.66	5 L2.Eq610b
113 Simple bar_1	Lower main gi	STEEL	13.54	16.70	0.64	5 L2.Eq610b
52 Simple bar_52	Lower main gi	STEEL	13.54	16.70	0.64	5 L2.Eq610b
104 Simple bar_1	Lower main gi	STEEL	13.54	16.70	0.60	5 L2.Eq610b
42 Simple bar_42	Lower main gi	STEEL	13.54	16.70	0.60	5 L2.Eq610b
103 Simple bar_1	Lower main gi	STEEL	13.54	16.70	0.58	5 L2.Eq610b
41 Simple bar_41	Lower main gi	STEEL	13.54	16.70	0.58	5 L2.Eq610b
93 Simple bar_93	Lower main gi	STEEL	13.54	16.70	0.48	5 L2.Eq610b
31 Simple bar_31	Lower main gi	STEEL	13.54	16.70	0.48	5 L2.Eq610b
92 Simple bar_92	Lower main gi	STEEL	13.54	16.70	0.46	5 L2.Eq610b
30 Simple bar_30	Lower main gi	STEEL	13.54	16.70	0.46	5 L2.Eq610b
6 Simple bar_6	Lower main gi	STEEL	13.54	16.70	0.35	8 L4.Eq610b/at supp
5 Simple bar_5	Lower main gi	STEEL	13.54	16.70	0.35	8 L4.Eq610b/at supp
82 Simple bar_82	Lower main gi	STEEL	13.54	16.70	0.31	5 L2.Eq610b
20 Simple bar_20	Lower main gi	STEEL	13.54	16.70	0.30	5 L2.Eq610b
19 Simple bar_19	Lower main gi	STEEL	13.54	16.70	0.30	5 L2.Eq610b
81 Simple bar_81	Lower main gi	STEEL	13.54	16.70	0.29	5 L2.Eq610b
69 Simple bar_69	Lower main gi	STEEL	13.54	16.70	0.28	5 L2.Eq610b
68 Simple bar_68	Lower main gi	STEEL	13.54	16.70	0.28	5 L2.Eq610b

Table 13, Utilization of lower main girder in order of utilization ratio

3.3.2.5 Upper main girders' utilization

The highest utilization ratio for the members is **0,79**.

The critical load combination was L2: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at midspan.

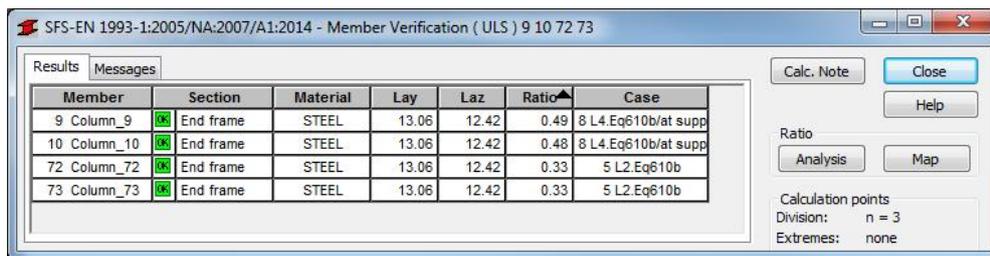
Member	Section	Material	Lay	Laz	Ratio	Case
54 Simple bar_54	Upper main gir	STEEL	14.49	11.90	0.79	5 L2.Eq610b
115 Simple bar_1	Upper main gir	STEEL	14.49	11.90	0.79	5 L2.Eq610b
55 Simple bar_55	Upper main gir	STEEL	14.49	11.90	0.76	5 L2.Eq610b
116 Simple bar_1	Upper main gir	STEEL	14.49	11.90	0.76	5 L2.Eq610b
105 Simple bar_1	Upper main gir	STEEL	14.49	11.90	0.72	5 L2.Eq610b
43 Simple bar_43	Upper main gir	STEEL	14.49	11.90	0.72	5 L2.Eq610b
106 Simple bar_1	Upper main gir	STEEL	14.49	11.90	0.70	5 L2.Eq610b
44 Simple bar_44	Upper main gir	STEEL	14.49	11.90	0.70	5 L2.Eq610b
21 Simple bar_21	Upper main gir	STEEL	14.49	11.90	0.64	8 L4.Eq610b/at supp
22 Simple bar_22	Upper main gir	STEEL	14.49	11.90	0.60	8 L4.Eq610b/at supp
94 Simple bar_94	Upper main gir	STEEL	14.49	11.90	0.60	5 L2.Eq610b
32 Simple bar_32	Upper main gir	STEEL	14.49	11.90	0.60	5 L2.Eq610b
95 Simple bar_95	Upper main gir	STEEL	14.49	11.90	0.58	5 L2.Eq610b
33 Simple bar_33	Upper main gir	STEEL	14.49	11.90	0.58	5 L2.Eq610b
7 Simple bar_7	Upper main gir	STEEL	14.49	11.90	0.52	8 L4.Eq610b/at supp
8 Simple bar_8	Upper main gir	STEEL	14.49	11.90	0.50	8 L4.Eq610b/at supp
83 Simple bar_83	Upper main gir	STEEL	14.49	11.90	0.45	5 L2.Eq610b
84 Simple bar_84	Upper main gir	STEEL	14.49	11.90	0.42	5 L2.Eq610b
70 Simple bar_70	Upper main gir	STEEL	14.49	11.90	0.38	5 L2.Eq610b
71 Simple bar_71	Upper main gir	STEEL	14.49	11.90	0.37	5 L2.Eq610b

Table 14, Utilization of upper main girder in order of utilization ratio

3.3.2.6 End columns' utilization

The highest utilization ratio for the members is **0,49**.

The critical load combination was L4: $1,25 \cdot \text{Selfweight} + 1,45 \cdot \text{TrafficLoad} + 1,50 \cdot 0,75 \cdot \text{Wind}$, and the traffic load's point loads were placed at support.



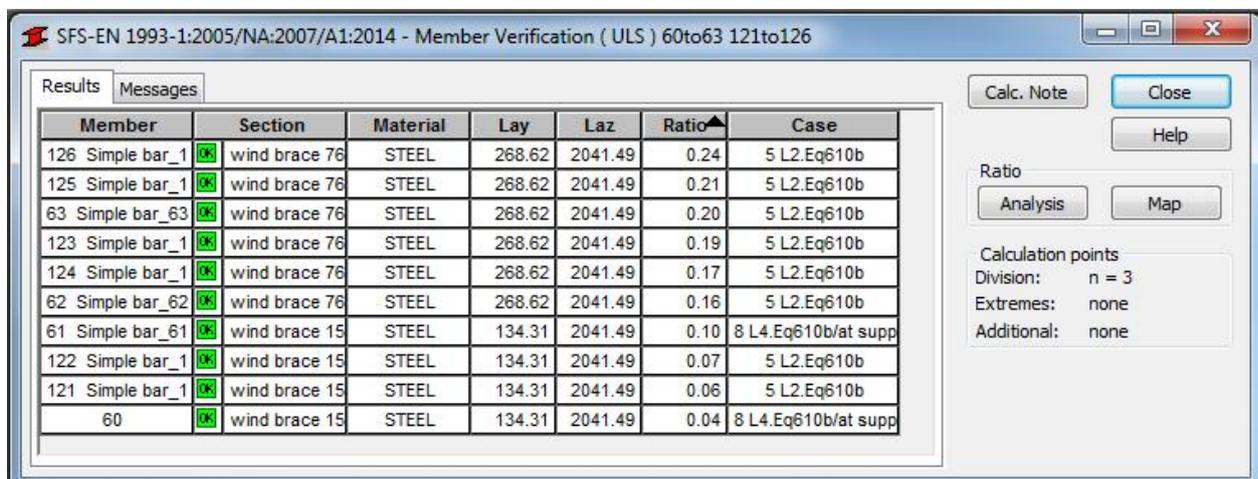
Member	Section	Material	Lay	Laz	Ratio	Case
9 Column_9	End frame	STEEL	13.06	12.42	0.49	8 L4.Eq610b/at supp
10 Column_10	End frame	STEEL	13.06	12.42	0.48	8 L4.Eq610b/at supp
72 Column_72	End frame	STEEL	13.06	12.42	0.33	5 L2.Eq610b
73 Column_73	End frame	STEEL	13.06	12.42	0.33	5 L2.Eq610b

Table 15, Utilization of end frame in order of utilization ratio

3.3.2.7 Wind bracings' utilization

The highest utilization ratio for the members is **0,24**.

The critical load combination was L2: 1,25*Seflweight+1,45*TrafficLoad+1,50*0,75*Wind, and the traffic load's point loads were placed at midspan.



Member	Section	Material	Lay	Laz	Ratio	Case
126 Simple bar_1	wind brace 76	STEEL	268.62	2041.49	0.24	5 L2.Eq610b
125 Simple bar_1	wind brace 76	STEEL	268.62	2041.49	0.21	5 L2.Eq610b
63 Simple bar_63	wind brace 76	STEEL	268.62	2041.49	0.20	5 L2.Eq610b
123 Simple bar_1	wind brace 76	STEEL	268.62	2041.49	0.19	5 L2.Eq610b
124 Simple bar_1	wind brace 76	STEEL	268.62	2041.49	0.17	5 L2.Eq610b
62 Simple bar_62	wind brace 76	STEEL	268.62	2041.49	0.16	5 L2.Eq610b
61 Simple bar_61	wind brace 15	STEEL	134.31	2041.49	0.10	8 L4.Eq610b/at supp
122 Simple bar_1	wind brace 15	STEEL	134.31	2041.49	0.07	5 L2.Eq610b
121 Simple bar_1	wind brace 15	STEEL	134.31	2041.49	0.06	5 L2.Eq610b
60	wind brace 15	STEEL	134.31	2041.49	0.04	8 L4.Eq610b/at supp

Table 16, Utilization of wind bracing in order of utilization ratio

4 CROSS GIRDER-RAIL BEARER JOINT

A connection verification was carried out for the cross girder-rail bearer joint of the 37-m span bridge. The result shows (Appendix 3), that the connection's resistance is not adequate against the design force. The basic requirement is that the resistance is greater than the forces, but analysis shows that $(V_{Ed}/V_{Rd}) = 1.284 > 1$. In addition, there are many uncertainties to the calculation, since the condition of these joints, especially the main plates under the cover plates is unknown and not visible.

The document IRS 77802 (former UIC 778-2) "Recommendations for determining the carrying capacity and fatigue risks of existing metallic railway bridges" gives instructions for Fatigue Susceptible Details, which generally have a more unreliable fatigue performance and experience indicates they are more prone to fatigue cracking than or other typical design details in modern bridges.

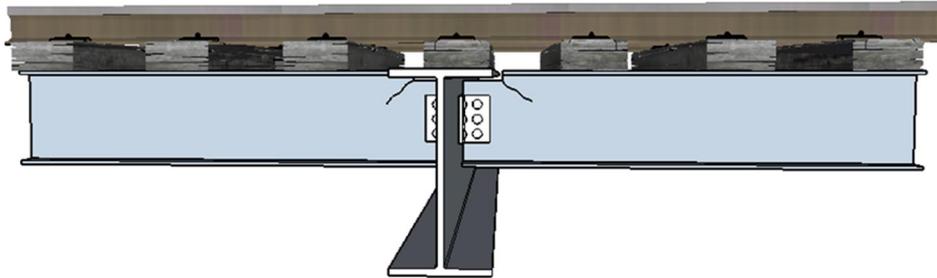
Typically Fatigue Susceptible Details:

- are subject to significant cycles of stress from short influence line length load effects that are neglected at the ULS (for example rail bearer joints that are assumed to be pinned joints at ULS subject to cycles of stress from passing individual axles) and or;
- are subject to significant cycles of stress from the real "whole bridge" behavior or the real distribution of stresses in complex details and or connections that is neglected at the ULS, for example cross girder end joints that have additional stresses induced by the differential global deflection of a bridge (particularly skew bridges) and / or;

- *have additional stress concentration features present that are not present in a similar detail tested to establish the fatigue performance of the detail.*

Examples of Fatigue Susceptible Details

- *An example of a Fatigue Susceptible Detail is a notched rail bearer to cross girder connection, especially where the notch has been flame cut:*



Picture 37. Joint of typical cross girder connection, one example (IRS 77802).

Joints that are Fatigue Susceptible Details include:

- *joints with other geometrical stress concentration features,*
- *misaligned load carrying parts*
- *joints subject to multiple cycles of stress due to the passage of individual axles*

An example of a fatigue susceptible joint is also a rail bearer to cross girder connection with flange plates providing continuity between adjoining rail bearers. This arrangement results in these joints being subject to multiple cycles of stress from the passage of individual axles as well as tension loading effects arising from the floor of a bridge being located below the neutral axis of the bridge superstructure.

Moreover, in case of a fatigue analysis wants to be performed, the dismantling of the joint is needed to gather sufficient information on the existing structure (conditions, presence of cracks in web). To ensure the safety of the structure, changing the critical fatigue sensitive connection parts (cross girders, rail bearers), is a suitable solution.

5 CONCLUSIONS

17 and 18 m spans

For the 17 and 18m bridges the deflection limit $L/600$ (EN 1990-1, A2.4.4.2.3 (1), [1]) is exceeded. Also, the tension and stresses are very high, utilization rate is over 0,9.

It is recommended to replace those structures for the whole span. In these spans the new structure is thought in the pre-engineering phase to be embedded rail, so the height of the secondary structures can be increased for capacity reasons compared to existing situation with wooden sleepers.

37 m spans

Truss bridge calculations show that utilizations are feasible and within limits, but deflection is at the limit. It is recommended renewing cross girders and rail bearers. The new structural parts are going to be constructed with pre-cambering, to prevent deflection from dead load and strengthen the bridge.

Joints of cross-girder – Rail bearer connection

Based on the studies and calculations, shows that the capacity of joints is not sufficient ($V_{Ed}/V_{Rd}) = 1.194 > 1$. There are many uncertainties to these calculations and to find a solution to save the secondary structures, more detailed

analysis is needed and the dismantling of the joint is needed to gather sufficient information on the existing structure (conditions, presence of cracks in web). To ensure the safety of the structure, changing the critical fatigue sensitive connection parts (cross girders, rail bearers), is a suitable solution.

LITERATURE

- [1] EN 1990: Basis of Structural design
- [2] EN 1991-2: Design of Steel Structures. Part 2: Traffic loads on bridges
- [3] EN 1993-1-1: Design of Steel Structures. Part 1-1: General rules and rules for buildings
- [4] EN 1993-1-8: Design of Steel Structures. Part 1-8: Design of joints
- [5] EN 1993-2: Design of Steel Structures. Part 2: Steel bridges
- [6] IRS 77802: Assessment of existing Steel Structures: Recommendations for Estimation of Remaining Fatigue Life; Eurocode Background Documents; JRC Scientific and Technical Reports
- [7] Riveted Connections in Historical Metal Structures (1840-1940): Hot Driven Rivets: Technology and Experiments. Quentin Collette, Thesis, Doctor in Engineering, Vrije Universiteit Brussel.

APPENDIX

- APPENDIX 1: 17m girder bridge calculation
- APPENDIX 2: 18m girder bridge calculation
- APPENDIX 3: 37m span bridge connection calculation

Preliminary calculation

References: EN1993-1-1, Design of steel structures
EN1991-2, Actions on structures - Part 2: Traffic loads on bridges

Material: Steel 355 $f_y := 355 \frac{\text{N}}{\text{mm}^2}$

$$\rho := 7850 \frac{\text{kg}}{\text{m}^3}$$

$$g := 9.8 \frac{\text{m}}{\text{s}^2}$$

Cross girder:

Geometry:

I - profile: $H := 570\text{mm}$

$$t_w := 10\text{mm}$$

$$b_f := 250\text{mm}$$

$$t_f := 20\text{mm}$$

$$h_w := H - 2 \cdot t_f = 530 \cdot \text{mm}$$

$$A_{\text{cross}} := h_w \cdot t_w + 2b_f \cdot t_f = 15300 \cdot \text{mm}^2$$

cross girder length: $l_{\text{cross}} := 4.775\text{m}$

Dynamic factor

For track with standard maintenance:

$$1 < \phi = \frac{2.16}{\sqrt{L\phi - 0.2}} + 0.73 < 2$$

Ref. EN1991-2
§6.4.5.2 (2)

Detenninant length L_{ϕ} :

Steel grillage: open deck without ballast bed ^b (for local and transverse stresses)		
3.1	Rail bearers: - as an element of a continuous grillage - simply supported	3 times cross girder spacing Cross girder spacing + 3 m
3.2	Cantilever of rail bearer ^a	3,6m
3.3	Cross girders (as part of cross girder/ continuous rail bearer grillage)	Twice the length of the cross girder
3.4	End cross girders	3,6m ^b

^a In general all cantilevers greater than 0,50 m supporting rail traffic actions need a special study in accordance with 6.4.6 and with the loading agreed with the relevant authority specified in the National Annex.
^b It is recommended to apply ϕ_3

Ref. EN1991-2 §6.4.5.3 Table 6.2

Cross girder length: $l_{\text{cross}} = 4.775 \text{ m}$

Dinamic factor for cross girder:

$$L_{\phi,\text{cross}} := 2 \cdot l_{\text{cross}} = 9.55 \text{ m}$$

$$\phi_{\text{cross}} := \frac{2.16}{\sqrt{\frac{L_{\phi,\text{cross}}}{\text{m}} - 0.2}} + 0.73 = 1.477$$

Loads:

Self weight:

$$G_{\text{cross}} := A_{\text{cross}} \cdot \rho \cdot g = 1177 \cdot \frac{\text{N}}{\text{m}}$$

$$\text{Rail self weight: } G_{\text{rail}} := 1 \frac{\text{kN}}{\text{m}}$$

Traffic Load: LM71-22,5

$$Q_v := 125 \text{ kN}$$

$$q_v := 40 \frac{\text{kN}}{\text{m}}$$

$$Q_{wv} := \phi_{\text{cross}} \cdot Q_v = 185 \cdot \text{kN}$$

$$q_{wv} := \phi_{\text{cross}} \cdot q_v = 59 \cdot \frac{\text{kN}}{\text{m}}$$

For cross girder, I calculated the load, which comes from traffic load and transferred by rails and longitudinal girders to the cross girder...

distance between cross girders: $L_{\text{cross}} := 1727 \text{mm}$

from distributed load - q.v: $F_{\text{traffic.q}} := q_v \cdot L_{\text{cross}} = 102 \cdot \text{kN}$

$n := 1$ number of pont loads, which carried by one cross girder

$$0 < L_{\text{cross}} - n \cdot 1.6 \text{m} = 0.127 \text{m} < 1.6 \text{m}$$

from point load - Q.v: $F_{\text{traffic.Q}} := (n + 1) \cdot Q_v = 369 \cdot \text{kN}$

For now I only work with these two cases, where the cross girder first only subjected to the distributed load (from LM71), then only the concentrated load (from LM71)

$$F_{\text{traffic}} := \max(F_{\text{traffic.q}}, F_{\text{traffic.Q}}) = 369.331 \cdot \text{kN}$$

Wind load:

height of the car: $H_{\text{car}} := 5 \text{m}$

Mean wind load: $q_{\text{mean}} := 1 \text{kPa}$

Longitudinal girder distance = gauge: $E := 1512 \text{mm}$

$$f_w := \frac{q_{\text{mean}} \cdot H_{\text{car}}^2}{2 \cdot E} = 8.267 \cdot \frac{\text{kN}}{\text{m}}$$

Load factors:

$\gamma_G := 1.35$ just permanent load

L1.Eq610.a $\gamma_G \cdot G_{\text{cross}} = 1.589 \cdot \frac{\text{kN}}{\text{m}}$ distributed load along girder axis

$\gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) = 2.331 \cdot \text{kN}$ concentrated load at 'rail position'

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_{0i} := 0.75$$

L2.Eq610.b concentrated load at 'rail position'

$$F_1 := \gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot F_{\text{traffic}} + \gamma_{\text{wind}} \cdot \psi_{0i} \cdot (f_w \cdot L_{\text{cross}}) = 554 \cdot \text{kN}$$

distributed load along girder axis

$$f := \gamma_G \cdot G_{\text{cross}} = 1.471 \cdot \frac{\text{kN}}{\text{m}}$$

concentrated load at 'rail position'

$$F_2 := \gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot F_{\text{traffic}} - \gamma_{\text{wind}} \cdot \psi_{0i} \cdot (f_w \cdot L_{\text{cross}}) = 522 \cdot \text{kN}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_{0i} := 0.8$$

L3.Eq610.b concentrated load at 'rail position'

$$\gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot \psi_{0i} \cdot F_{\text{traffic}} + \gamma_{\text{wind}} \cdot (f_w \cdot L_{\text{cross}}) = 452 \cdot \text{kN}$$

distributed load along girder axis

$$\gamma_G \cdot G_{\text{cross}} = 1.471 \cdot \frac{\text{kN}}{\text{m}}$$

concentrated load at 'rail position'

$$\gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot \psi_{0i} \cdot F_{\text{traffic}} - \gamma_{\text{wind}} \cdot (f_w \cdot L_{\text{cross}}) = 409 \cdot \text{kN}$$

I only calculate the design moment for L2 load combination (the most relevant one)

I assume that the cross girder is a simply supported beam.

cross girder length: $l_{\text{cross}} = 4.775 \text{ m}$

$$l_1 := \frac{(l_{\text{cross}} - E)}{2} = 1.632 \text{ m}$$

$$l_2 := l_1 = 1.632 \text{ m}$$

Calc of reaction forces: $B_1 := \frac{F_1 \cdot l_1 + F_2 \cdot (l_1 + E)}{l_{\text{cross}}} = 533 \cdot \text{kN}$

$$B_2 := \frac{f \cdot l_{\text{cross}}}{2} = 3.513 \cdot \text{kN}$$

$$B := B_1 + B_2 = 536 \cdot \text{kN}$$

$$A_1 := F_1 + F_2 - B_1 = 5.428 \times 10^5 \text{ N}$$

$$A_2 := B_2 = 3.513 \times 10^3 \text{ N}$$

$$A := A_1 + A_2 = 546 \cdot \text{kN}$$

bending moment at midsection:

$$M_{\text{Ed.mid}} := f \cdot \frac{l_{\text{cross}}^2}{8} + \left[A_1 \cdot \frac{l_{\text{cross}}}{2} - F_1 \cdot \left(\frac{l_{\text{cross}}}{2} - l_1 \right) \right] = 881 \cdot \text{kN} \cdot \text{m}$$

bending moment at rail position 1:

$$M_{\text{Ed.1}} := \left(A_2 \cdot l_1 - f \cdot \frac{l_1^2}{2} \right) + (A_1 \cdot l_1) = 889 \cdot \text{kN} \cdot \text{m}$$

bending moment at rail position 2:

$$M_{\text{Ed.2}} := \left[A_2 \cdot (l_1 + E) - f \cdot \frac{(l_1 + E)^2}{2} \right] + [A_1 \cdot (l_1 + E) - F_1 \cdot E] = 873 \text{ m} \cdot \text{kN}$$

check:

$$M_{\text{Ed.3}} := \left(B_2 \cdot l_2 - f \cdot \frac{l_2^2}{2} \right) + B_1 \cdot l_2 = 873 \text{ m} \cdot \text{kN}$$

$$M_{\text{Ed}} := \max(M_{\text{Ed.mid}}, M_{\text{Ed.1}}, M_{\text{Ed.2}}) = 889 \cdot \text{kN} \cdot \text{m}$$

Cross section resistance:

Cross section classification:

$$\varepsilon := \sqrt{\frac{235 \text{ MPa}}{f_y}} = 0.814$$

web:

$$\frac{h_w}{t_w} = 53$$

$$72 \cdot \varepsilon = 58.58 \quad \text{Class 1}$$

$$83 \cdot \varepsilon = 67.53 \quad \text{Class 2}$$

$$124 \cdot \varepsilon = 100.888 \quad \text{Class 3}$$

=> Class 1

$$\text{flange: } \frac{b_f - t_w}{t_f} = 6 \quad \begin{array}{l} 9 \cdot \epsilon = 7.323 \quad \text{Class 1} \\ 10 \epsilon = 8.136 \quad \text{Class 2} \\ 14 \cdot \epsilon = 11.391 \quad \text{Class 3} \end{array} \quad \Rightarrow \text{Class 1}$$

Cross section is Class 1 - plastic analysis

$$\text{plastic section modulus: } W_{pl} := b_f \cdot t_f \cdot (H - t_f) + \frac{t_w \cdot h_w^2}{4} = 3452250 \cdot \text{mm}^3$$

$$\text{elastic section modulus: } W_{el} := \frac{b_f \cdot H^2}{6} - \frac{(b_f - t_w) \cdot h_w^3}{6 \cdot H} = 3089991 \cdot \text{mm}^3$$

Moment resistance of cross girder:

$$M_{pl.Rd} := \frac{W_{pl} \cdot f_y}{\gamma_{M0}} = 1226 \cdot \text{kN} \cdot \text{m}$$

$$\gamma_{M0} := 1$$

$$\frac{M_{Ed}}{M_{pl.Rd}} = 0.726 < 1 \quad \text{OK!}$$

Longitudinal girder/Railbearer:

Geometry:

I - profile:

$$H_{long} := 374 \text{mm}$$

$$t_w := 10 \text{mm}$$

$$b_{f,1} := 400 \text{mm}$$

$$t_{f,1} := 20 \text{mm}$$

$$b_{f,2} := 200 \text{mm}$$

$$t_{f,2} := 12 \text{mm}$$

$$h_w := H_{long} - 2 \cdot t_f = 334 \cdot \text{mm}$$

$$A_{long} := h_w \cdot t_w + b_{f,1} \cdot t_{f,1} + b_{f,2} \cdot t_{f,2} = 13740 \cdot \text{mm}^2$$

long. girder length: $L_{\text{long}} := L_{\text{cross}} = 1.727 \text{ m}$

Dinamic factor for rail bearer:

$$L_{\phi,\text{rail}} := 3 \cdot L_{\text{long}} = 5.181 \text{ m}$$

$$\phi_{\text{rail}} := \frac{2.16}{\sqrt{\frac{L_{\phi,\text{rail}}}{\text{m}} - 0.2}} + 0.73 = 1.77$$

Loads:

Self weight:

$$G_{\text{long}} := A_{\text{long}} \cdot \rho \cdot g = 1057 \cdot \frac{\text{N}}{\text{m}}$$

Traffic Load: LM71-22,5

$$Q_v := 125 \text{ kN}$$

$$q_v := 40 \frac{\text{kN}}{\text{m}}$$

$$Q_v := \phi_{\text{rail}} \cdot Q_v = 221 \cdot \text{kN}$$

$$q_v := \phi_{\text{rail}} \cdot q_v = 71 \cdot \frac{\text{kN}}{\text{m}}$$

In this preliminary calculation I'll only check the beam against the maximum positive bending moment:

During calculation I assume, the longitudinal girder is a simply supported beam.

long. girder length: $L_{\text{long}} := L_{\text{cross}} = 1.727 \text{ m}$

I get the maximum positive bending moment, when the concentrated loads are positiond in the middle of the beam.

$$\gamma_G := 1.35$$

$$\text{L1.Eq610.a} \quad \gamma_G \cdot G_{\text{long}} + \gamma_G \cdot G_{\text{rail}} = 2.777 \cdot \frac{\text{kN}}{\text{m}}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{wind} := 1.5 \quad \psi_{0i} := 0.75$$

L2.Eq610.b

$$n := 1$$

$$0\text{m} < n \cdot 1.6\text{m} = 1.6\text{m} < L_{long} = 1.727\text{m}$$

$$F := \gamma_Q \cdot Q_v = 321 \cdot \text{kN}$$

$$f_1 := \gamma_G \cdot G_{long} + \gamma_{wind} \cdot \psi_{0i} \cdot f_w = 10.622 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

$$f_2 := \gamma_G \cdot G_{long} - \gamma_{wind} \cdot \psi_{0i} \cdot f_w = -7.979 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

$$\psi_{0i} := 0.8$$

L3.Eq610.b

$$\gamma_Q \cdot \psi_{0i} \cdot Q_v = 257 \cdot \text{kN}$$

$$\gamma_G \cdot G_{long} + \gamma_{wind} \cdot f_w = 13.722 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

$$\gamma_G \cdot G_{long} - \gamma_{wind} \cdot f_w = -11.08 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

Calc of reaction forces:

$$R_y := \frac{(n + 1) \cdot F + f_1 \cdot L_{long}}{2} = 330.052 \cdot \text{kN}$$

Maximum moment at mid span:

long. girder length: $L_{long} = 1.727\text{m}$

$$l_1 := \frac{(L_{cross} - 1.6\text{m})}{2} = 0.064\text{m}$$

$$l_2 := l_1 = 0.064\text{m}$$

$$M_{Ed1} := R_y \cdot \frac{L_{long}}{2} - F \cdot \left(\frac{L_{long}}{2} - l_1 \right) - f_1 \cdot \frac{L_{long}^2}{8} = 24 \cdot \text{kN} \cdot \text{m}$$

Cross section classification:

web:

$$\frac{h_w}{t_w} = 33.4 \quad 72 \cdot \epsilon = 58.58 \quad \text{Class 1}$$

$$\epsilon := \sqrt{\frac{235\text{MPa}}{f_y}} = 0.814$$

$83 \cdot \varepsilon = 67.53$ Class 2 \Rightarrow Class 1

$124 \cdot \varepsilon = 100.888$ Class 3

upper flange: $\frac{b_{f.1} - t_w}{2} = 9.75$
 $t_{f.1}$

$9 \cdot \varepsilon = 7.323$ Class 1

$10\varepsilon = 8.136$ Class 2 \Rightarrow Class 3

$14 \cdot \varepsilon = 11.391$ Class 3

Class 4

lower flange: $\frac{b_{f.2} - t_w}{2} = 7.917$
 $t_{f.2}$

$9 \cdot \varepsilon = 7.323$ Class 1

$10\varepsilon = 8.136$ Class 2 \Rightarrow Class 2

$14 \cdot \varepsilon = 11.391$ Class 3

Class 4

Cross section is Class 3 - elastic analysis

plastic section modulus: $W_{pl} := b_f \cdot t_f \cdot (H_{long} - t_f) + \frac{t_w \cdot h_w^2}{4} = 2048890 \cdot \text{mm}^3$ $\gamma_{M0} := 1$

elastic section modulus (from Robot Str. Analysis) : $W_{el} := 1282.6 \text{cm}^3$

Moment resistance of cross girder:

$$f_y = 355 \cdot \frac{\text{N}}{\text{mm}^2}$$

$$M_{el.Rd} := \frac{W_{el} \cdot f_y}{\gamma_{M0}} = 455 \cdot \text{kN} \cdot \text{m}$$

$$\frac{M_{Ed}}{M_{el.Rd}} = 0.053 < 1 \quad \text{OK!}$$

Main girder:

Geometry:

I - profile: $H := 1700 \text{mm}$
 $t_w := 20 \text{mm}$

$$b_f := 400\text{mm}$$

$$t_f := 30\text{mm}$$

$$h_w := H - 2 \cdot t_f = 1.64 \times 10^3 \cdot \text{mm}$$

$$A_{\text{main}} := h_w \cdot t_w + 2b_f \cdot t_f = 56800 \cdot \text{mm}^2$$

Span: $L := 17.27\text{m}$

Dinamic factor for main girder

$$L_{\phi,\text{main}} := L = 17.27 \text{ m}$$

$$\phi_{\text{main}} := \frac{2.16}{\sqrt{\frac{L_{\phi,\text{main}}}{\text{m}} - 0.2}} + 0.73 = 1.276$$

Case	Structural element	Determinant length L_{ϕ}
Main girders		
5.1	Simply supported girders and slabs (including steel beams embedded in concrete)	Span in main girder direction

Ref. EN1991-2 §6.4.5.3 Table 6.2

Loads:

Permanent load:

$$G_{\text{main}} := A_{\text{main}} \cdot \rho \cdot g = 4.37 \cdot \frac{\text{kN}}{\text{m}} \quad \text{self weight of main girder}$$

$$G_{\text{cross}} := \frac{G_{\text{cross}}}{2} = 0.589 \cdot \frac{\text{kN}}{\text{m}} \quad \text{self weight of cross girder}$$

$$G_{\text{long}} = 1.057 \cdot \frac{\text{kN}}{\text{m}} \quad \text{self weight of railbearer}$$

Rail self weight: $G_{\text{rail}} := 1 \frac{\text{kN}}{\text{m}}$

Traffic Load: LM71-22,5

$$Q_{wv} := 125 \text{ kN}$$

$$q_{wv} := 40 \frac{\text{kN}}{\text{m}}$$

$$Q_{wv} := \phi_{\text{main}} \cdot Q_v = 160 \cdot \text{kN}$$

$$q_{wv} := \phi_{\text{main}} \cdot q_v = 51 \cdot \frac{\text{kN}}{\text{m}}$$

Wind load:

height of the car: $H_{\text{car}} := 5 \text{ m}$

Mean wind load: $q_{\text{mean}} := 1 \text{ kPa}$

Longitudinal girder distance = gauge: $E := 1512 \text{ mm}$

$$f_{wv} := \frac{q_{\text{mean}} \cdot H_{\text{car}}^2}{2 \cdot E} = 8.267 \cdot \frac{\text{kN}}{\text{m}}$$

Load factors:

$$\gamma_G := 1.35 \quad \text{just permanent load}$$

L1.Eq610.a distributed load along girder axis

$$\gamma_G \cdot (G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}}) = 9.47 \cdot \frac{\text{kN}}{\text{m}}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_{0i} := 0.75$$

L2.Eq610.b

concentrated load at 'rail position'

$$F_{2i} := \gamma_Q \cdot Q_v \cdot 4 = 925 \cdot \text{kN}$$

distributed load along girder axis

$$f_{2i} := \gamma_G \cdot (G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}}) + \gamma_Q \cdot q_v + \gamma_{\text{wind}} \cdot \psi_{0i} \cdot f_w = 92.08 \cdot \frac{\text{kN}}{\text{m}}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_{0i} := 0.8$$

L3.Eq610.b

concentrated load at 'rail position'

$$F_3 := \gamma_Q \cdot \psi_{0i} \cdot Q_V \cdot 4 = 740 \cdot \text{kN}$$

distributed load along girder axis

$$f_3 := \gamma_G \cdot (G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}}) + \gamma_Q \cdot \psi_{0i} \cdot q_V + \gamma_{\text{wind}} \cdot f_W = 80.378 \cdot \frac{\text{kN}}{\text{m}}$$

I only calculate the design moment for L2 load combination (the most relevant one)

I assume that the main girder is a simply supported beam.

$$M_{Ed} := \frac{f_2 \cdot L^2}{8} + \frac{F_2 \cdot L}{4} = 7427 \cdot \text{kN} \cdot \text{m}$$

Cross section resistance:

Cross section classification:

web:	$\frac{h_w}{t_w} = 82$	$72 \cdot \epsilon = 58.58$	Class 1	
		$83 \cdot \epsilon = 67.53$	Class 2	=> Class 3
		$124 \cdot \epsilon = 100.888$	Class 3	

flange:	$\frac{b_f - t_w}{2} = 6.333$	$9 \cdot \epsilon = 7.323$	Class 1	
		$10 \epsilon = 8.136$	Class 2	=> Class 1
		$14 \cdot \epsilon = 11.391$	Class 3	

Cross section is Class 3 - elastic analysis

plastic section modulus: $W_{pl} := b_f \cdot t_f \cdot (H - t_f) + \frac{t_w \cdot h_w^2}{4} = 33488000 \cdot \text{mm}^3$

elastic section modulus:
$$W_{el} := \frac{b_f \cdot H^2}{6} - \frac{(b_f - t_w) \cdot h_w^3}{6 \cdot H} = 28337380 \cdot \text{mm}^3$$

Moment resistance of cross girder:

$$\gamma_{M0} := 1$$

$$M_{el.Rd} := \frac{W_{el} \cdot f_y}{\gamma_{M0}} = 10060 \cdot \text{kN} \cdot \text{m}$$

$$\frac{M_{Ed}}{M_{el.Rd}} = 0.738 < 1 \quad \text{OK!}$$

Deflection of main girder:

second moment of area:
$$I := \frac{h_w^3 \cdot t_w}{12} + \left(\frac{b_f}{12} \right) \cdot (H^3 - h_w^3) = 2.409 \times 10^{10} \cdot \text{mm}^4$$

modulus of elasticity:
$$E_a := 210000 \frac{\text{N}}{\text{mm}^2}$$

permanent characteristic:
$$g_k := G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}} = 7.015 \cdot \frac{\text{kN}}{\text{m}}$$

variable characteristic:
$$q_k := q_v + f_w = 59.309 \cdot \frac{\text{kN}}{\text{m}}$$

$$Q_k := 4Q_v = 638.022 \cdot \text{kN}$$

the calculation of deflection is an approximation on the safe side

$$\delta_{\max} := \frac{5 \cdot (g_k + q_k) \cdot L^4}{384 \cdot E_a \cdot I} + \frac{Q_k \cdot L^3}{48 \cdot E_a \cdot I} = 28.72 \cdot \text{mm} < \frac{L}{400} = 43.175 \cdot \text{mm}$$

Total weight of structure:

$$n_{\text{cross}} := 11$$

$$A_{\text{cross}} \cdot l_{\text{cross}} \cdot \rho \cdot n_{\text{cross}} = 6.309 \times 10^3 \text{ kg}$$

$$n_{\text{long}} := 2$$

$$A_{\text{long}} \cdot L \cdot \rho \cdot n_{\text{long}} = 3.725 \times 10^3 \text{ kg}$$

$$n_{\text{main}} := 2$$

$$A_{\text{main}} \cdot L \cdot \rho \cdot n_{\text{main}} = 1.54 \times 10^4 \text{ kg}$$

Buckling support girder:

Geometry:

$$\text{I - profile: } h_b := 246 \text{ mm}$$

$$t_{w,b} := 10 \text{ mm}$$

$$b_{f,b} := 120 \text{ mm}$$

$$t_{f,b} := 13 \text{ mm}$$

$$h_{w,b} := h_b - 2 \cdot t_{f,b} = 220 \cdot \text{mm}$$

$$A_{\text{buckl}} := h_{w,b} \cdot t_{w,b} + 2b_{f,b} \cdot t_{f,b} = 5320 \cdot \text{mm}^2$$

$$l_{\text{buckl}} := E = 1.512 \text{ m}$$

$$n_{\text{buckl}} := n_{\text{cross}} - 1 = 10$$

Wind bracing:

$$A_w := 102 \text{ mm} \cdot 13 \text{ mm} = 1.326 \times 10^{-3} \text{ m}^2$$

$$L_w := 5297 \text{ mm}$$

$$n_w := 10$$

$$G_{\text{TOT}} := A_{\text{main}} \cdot L \cdot \rho \cdot n_{\text{main}} + A_{\text{long}} \cdot L \cdot \rho \cdot n_{\text{long}} + A_{\text{cross}} \cdot l_{\text{cross}} \cdot \rho \cdot n_{\text{cross}} \dots = 26.617 \cdot \text{tonne} \\ + A_{\text{buckl}} \cdot l_{\text{buckl}} \cdot \rho \cdot n_{\text{buckl}} + A_w \cdot L_w \cdot \rho \cdot n_w$$

$$G_{\text{TOT}} \cdot g = 260.85 \cdot \text{kN}$$

$$\text{Side walk: } g_{\text{sw}} := 80 \frac{\text{kg}}{\text{m}}$$

$$L = 17.27 \text{ m}$$

$$G_{\text{TOT}} \cdot g + g_{\text{sw}} \cdot L \cdot g = 274.39 \cdot \text{kN}$$

$$G_{\text{TOT}} + g_{\text{sw}} \cdot L = 27999.07 \cdot \text{kg}$$

Preliminary calculation

References: EN1993-1-1, Design of steel structures
EN1991-2, Actions on structures - Part 2: Traffic loads on bridges

Material: Steel 355

$$f_y := 355 \frac{\text{N}}{\text{mm}^2}$$

$$\rho := 7850 \frac{\text{kg}}{\text{m}^3}$$

$$g := 9.8 \frac{\text{m}}{\text{s}^2}$$

Cross girder:

Geometry:

I - profile: $H := 490\text{mm}$

$$t_w := 10\text{mm}$$

$$b_f := 250\text{mm}$$

$$t_f := 20\text{mm}$$

$$h_w := H - 2 \cdot t_f = 450 \cdot \text{mm}$$

$$A_{\text{cross}} := h_w \cdot t_w + 2b_f \cdot t_f = 14500 \cdot \text{mm}^2$$

cross girder length: $l_{\text{cross}} := 4.775\text{m}$

Dynamic factor

For track with standard maintenance:

$$1 < \phi = \frac{2.16}{\sqrt{L\phi - 0.2}} + 0.73 < 2$$

Ref. EN1991-2
§6.4.5.2 (2)

Detenninant length L_{ϕ} :

Steel grillage: open deck without ballast bed ^b (for local and transverse stresses)		
3.1	Rail bearers: - as an element of a continuous grillage - simply supported	3 times cross girder spacing Cross girder spacing + 3 m
3.2	Cantilever of rail bearer ^a	3,6m
3.3	Cross girders (as part of cross girder/ continuous rail bearer grillage)	Twice the length of the cross girder
3.4	End cross girders	3,6m ^b

^a In general all cantilevers greater than 0,50 m supporting rail traffic actions need a special study in accordance with 6.4.6 and with the loading agreed with the relevant authority specified in the National Annex.
^b It is recommended to apply ϕ_3

Ref. EN1991-2 §6.4.5.3 Table 6.2

Cross girder length: $l_{\text{cross}} = 4.775 \text{ m}$

Dinamic factor for cross girder:

$$L_{\phi,\text{cross}} := 2 \cdot l_{\text{cross}} = 9.55 \text{ m}$$

$$\phi_{\text{cross}} := \frac{2.16}{\sqrt{\frac{L_{\phi,\text{cross}}}{\text{m}} - 0.2}} + 0.73 = 1.477$$

Loads:

Self weight:

$$G_{\text{cross}} := A_{\text{cross}} \cdot \rho \cdot g = 1115 \cdot \frac{\text{N}}{\text{m}}$$

Rail self weight: $G_{\text{rail}} := 1 \frac{\text{kN}}{\text{m}}$

Traffic Load: LM71-22,5

$$Q_v := 125 \text{ kN}$$

$$q_v := 40 \frac{\text{kN}}{\text{m}}$$

$$Q_v := \phi_{\text{cross}} \cdot Q_v = 185 \cdot \text{kN}$$

$$q_v := \phi_{\text{cross}} \cdot q_v = 59 \cdot \frac{\text{kN}}{\text{m}}$$

For cross girder, I calculated the load, which comes from traffic load and transferred by rails and longitudinal girders to the cross girder.

distance between cross girders: $L_{\text{cross}} := 1867 \text{mm}$

from distributed load - q.v: $F_{\text{traffic.q}} := q_v \cdot L_{\text{cross}} = 110 \cdot \text{kN}$

$n := 1$ number of pont loads, which carried by one cross girder

$$0 < L_{\text{cross}} - n \cdot 1.6 \text{m} = 0.267 \text{m} < 1.6 \text{m}$$

from point load - Q.v: $F_{\text{traffic.Q}} := (n + 1) \cdot Q_v = 369 \cdot \text{kN}$

For now I only work with these two cases, where the cross girder first only subjected to the distributed load (from LM71), then only the concentrated load (from LM71)

$$F_{\text{traffic}} := \max(F_{\text{traffic.q}}, F_{\text{traffic.Q}}) = 369.331 \cdot \text{kN}$$

Wind load:

height of the car: $H_{\text{car}} := 5 \text{m}$

Mean wind load: $q_{\text{mean}} := 1 \text{kPa}$

Longitudinal girder distance = gauge: $E := 1512 \text{mm}$

$$f_w := \frac{q_{\text{mean}} \cdot H_{\text{car}}^2}{2 \cdot E} = 8.267 \cdot \frac{\text{kN}}{\text{m}}$$

Load factors:

$\gamma_G := 1.35$ just permanent load

L1.Eq610.a $\gamma_G \cdot G_{\text{cross}} = 1.506 \cdot \frac{\text{kN}}{\text{m}}$ distributed load along girder axis

$\gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) = 2.52 \cdot \text{kN}$ concentrated load at 'rail position'

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_{0i} := 0.75$$

L2.Eq610.b concentrated load at 'rail position'

$$F_1 := \gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot F_{\text{traffic}} + \gamma_{\text{wind}} \cdot \psi_{0i} \cdot (f_w \cdot L_{\text{cross}}) = 555 \cdot \text{kN}$$

distributed load along girder axis

$$f := \gamma_G \cdot G_{\text{cross}} = 1.394 \cdot \frac{\text{kN}}{\text{m}}$$

concentrated load at 'rail position'

$$F_2 := \gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot F_{\text{traffic}} - \gamma_{\text{wind}} \cdot \psi_{0i} \cdot (f_w \cdot L_{\text{cross}}) = 520 \cdot \text{kN}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_{0i} := 0.8$$

L3.Eq610.b concentrated load at 'rail position'

$$\gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot \psi_{0i} \cdot F_{\text{traffic}} + \gamma_{\text{wind}} \cdot (f_w \cdot L_{\text{cross}}) = 454 \cdot \text{kN}$$

distributed load along girder axis

$$\gamma_G \cdot G_{\text{cross}} = 1.394 \cdot \frac{\text{kN}}{\text{m}}$$

concentrated load at 'rail position'

$$\gamma_G \cdot (G_{\text{rail}} \cdot L_{\text{cross}}) + \gamma_Q \cdot \psi_{0i} \cdot F_{\text{traffic}} - \gamma_{\text{wind}} \cdot (f_w \cdot L_{\text{cross}}) = 408 \cdot \text{kN}$$

I only calculate the design moment for L2 load combination (the most relevant one)

I assume that the cross girder is a simply supported beam.

cross girder length: $l_{\text{cross}} = 4.775 \text{ m}$

$$l_1 := \frac{(l_{\text{cross}} - E)}{2} = 1.632 \text{ m}$$

$$l_2 := l_1 = 1.632 \text{ m}$$

Calc of reaction forces: $B_1 := \frac{F_1 \cdot l_1 + F_2 \cdot (l_1 + E)}{l_{\text{cross}}} = 532 \cdot \text{kN}$

$$B_2 := \frac{f \cdot l_{\text{cross}}}{2} = 3.329 \cdot \text{kN}$$

$$B := B_1 + B_2 = 536 \cdot \text{kN}$$

$$A_1 := F_1 + F_2 - B_1 = 5.434 \times 10^5 \text{ N}$$

$$A_2 := B_2 = 3.329 \times 10^3 \text{ N}$$

$$\underline{A} := A_1 + A_2 = 547 \cdot \text{kN}$$

bending moment at midsection:

$$M_{\text{Ed.mid}} := f \cdot \frac{l_{\text{cross}}^2}{8} + \left[A_1 \cdot \frac{l_{\text{cross}}}{2} - F_1 \cdot \left(\frac{l_{\text{cross}}}{2} - l_1 \right) \right] = 881 \cdot \text{kN} \cdot \text{m}$$

bending moment at rail position 1:

$$M_{\text{Ed.1}} := \left(A_2 \cdot l_1 - f \cdot \frac{l_1^2}{2} \right) + (A_1 \cdot l_1) = 890 \cdot \text{kN} \cdot \text{m}$$

bending moment at rail position 2:

$$M_{\text{Ed.2}} := \left[A_2 \cdot (l_1 + E) - f \cdot \frac{(l_1 + E)^2}{2} \right] + \left[A_1 \cdot (l_1 + E) - F_1 \cdot E \right] = 872 \text{ m} \cdot \text{kN}$$

check:

$$M_{\text{Ed.3}} := \left(B_2 \cdot l_2 - f \cdot \frac{l_2^2}{2} \right) + B_1 \cdot l_2 = 872 \text{ m} \cdot \text{kN}$$

$$M_{\text{Ed}} := \max(M_{\text{Ed.mid}}, M_{\text{Ed.1}}, M_{\text{Ed.2}}) = 890 \cdot \text{kN} \cdot \text{m}$$

Cross section resistance:

Cross section classification:

$$\underline{\varepsilon} := \sqrt{\frac{235 \text{ MPa}}{f_y}} = 0.814$$

web:

$$\frac{h_w}{t_w} = 45$$

$$72 \cdot \varepsilon = 58.58 \quad \text{Class 1}$$

$$83 \cdot \varepsilon = 67.53 \quad \text{Class 2}$$

=> Class 1

$$124 \cdot \varepsilon = 100.888 \quad \text{Class 3}$$

$$\text{flange: } \frac{b_f - t_w}{t_f} = 6 \quad 9 \cdot \varepsilon = 7.323 \quad \text{Class 1}$$

$$10\varepsilon = 8.136 \quad \text{Class 2} \quad \Rightarrow \text{Class 1}$$

$$14 \cdot \varepsilon = 11.391 \quad \text{Class 3}$$

Cross section is Class 1 - plastic analysis

$$\text{plastic section modulus: } W_{pl} := b_f \cdot t_f \cdot (H - t_f) + \frac{t_w \cdot h_w^2}{4} = 2856250 \cdot \text{mm}^3$$

$$\text{elastic section modulus: } W_{el} := \frac{b_f \cdot H^2}{6} - \frac{(b_f - t_w) \cdot h_w^3}{6 \cdot H} = 2565391 \cdot \text{mm}^3$$

Moment resistance of cross girder:

$$\gamma_{M0} := 1$$

$$M_{pl.Rd} := \frac{W_{pl} \cdot f_y}{\gamma_{M0}} = 1014 \cdot \text{kN} \cdot \text{m}$$

$$\frac{M_{Ed}}{M_{pl.Rd}} = 0.878 < 1 \quad \text{OK!}$$

Longitudinal girder/Railbearer:

Geometry:

I - profile:

$$H_{long} := 374 \text{mm}$$

$$t_{ww} := 10 \text{mm}$$

$$b_{f,1} := 400 \text{mm}$$

$$t_{f,1} := 20 \text{mm}$$

$$b_{f,2} := 200 \text{mm}$$

$$t_{f,2} := 12 \text{mm}$$

$$h_{ww} := H_{long} - 2 \cdot t_f = 334 \cdot \text{mm}$$

$$A_{long} := h_w \cdot t_w + b_{f,1} \cdot t_{f,1} + b_{f,2} \cdot t_{f,2} = 13740 \cdot \text{mm}^2$$

long. girder length: $L_{long} := L_{cross} = 1.867 \text{ m}$

Dinamic factor for rail bearer:

$$L_{\phi, rail} := 3 \cdot L_{long} = 5.601 \text{ m}$$

$$\phi_{rail} := \frac{2.16}{\sqrt{\frac{L_{\phi, rail}}{\text{m}} - 0.2}} + 0.73 = 1.727$$

Loads:

Self weight:

$$G_{long} := A_{long} \cdot \rho \cdot g = 1057 \cdot \frac{\text{N}}{\text{m}}$$

Traffic Load: LM71-22,5

$$Q_{ww} := 125 \text{ kN}$$

$$q_{ww} := 40 \frac{\text{kN}}{\text{m}}$$

$$Q_{vv} := \phi_{rail} \cdot Q_v = 216 \cdot \text{kN}$$

$$q_{vv} := \phi_{rail} \cdot q_v = 69 \cdot \frac{\text{kN}}{\text{m}}$$

In this preliminary calculation I'll only check the beam against the maximum positive bending moment:

During calculation I assume, the longitudinal girder is a simply supported beam.

long. girder length: $L_{long} := L_{cross} = 1.867 \text{ m}$

I get the maximum positive bending moment, when the concentrated loads are positiond in the middle of the beam.

$$\gamma_{Gv} := 1.35$$

$$L1.Eq610.a \quad \gamma_G \cdot G_{long} + \gamma_G \cdot G_{rail} = 2.777 \cdot \frac{\text{kN}}{\text{m}}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{wind} := 1.5 \quad \psi_{0i} := 0.75$$

$$L2.Eq610.b \quad n := 1$$

$$0\text{m} < n \cdot 1.6\text{m} = 1.6\text{m} < L_{long} = 1.867\text{m}$$

$$F := \gamma_Q \cdot Q_v = 313 \cdot \text{kN}$$

$$f_1 := \gamma_G \cdot G_{long} + \gamma_{wind} \cdot \psi_{0i} \cdot f_w = 10.622 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

$$f_2 := \gamma_G \cdot G_{long} - \gamma_{wind} \cdot \psi_{0i} \cdot f_w = -7.979 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

$$\psi_{0i} := 0.8$$

$$L3.Eq610.b \quad \gamma_Q \cdot \psi_{0i} \cdot Q_v = 250 \cdot \text{kN}$$

$$\gamma_G \cdot G_{long} + \gamma_{wind} \cdot f_w = 13.722 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

$$\gamma_G \cdot G_{long} - \gamma_{wind} \cdot f_w = -11.08 \cdot \frac{\text{kN}}{\text{m}} \quad \text{distributed load}$$

$$\text{Calc of reaction forces:} \quad R_y := \frac{(n + 1) \cdot F + f_1 \cdot L_{long}}{2} = 322.922 \cdot \text{kN}$$

Maximum moment at mid span:

$$\text{long. girder length:} \quad L_{long} = 1.867\text{m}$$

$$l_1 := \frac{(L_{cross} - 1.6\text{m})}{2} = 0.133\text{m}$$

$$l_2 := l_1 = 0.133\text{m}$$

$$M_{Ed} := R_y \cdot \frac{L_{long}}{2} - F \cdot \left(\frac{L_{long}}{2} - l_1 \right) - f_1 \cdot \frac{L_{long}^2}{8} = 46 \cdot \text{kN} \cdot \text{m}$$

Cross section classification:

$$\varepsilon := \sqrt{\frac{235 \text{ MPa}}{f_y}} = 0.814$$

web:	$\frac{h_w}{t_w} = 33.4$	$72 \cdot \varepsilon = 58.58$	Class 1	=> Class 1
		$83 \cdot \varepsilon = 67.53$	Class 2	
		$124 \cdot \varepsilon = 100.888$	Class 3	
upper flange:	$\frac{b_{f,1} - t_w}{2 t_{f,1}} = 9.75$	$9 \cdot \varepsilon = 7.323$	Class 1	=> Class 3
		$10 \varepsilon = 8.136$	Class 2	
		$14 \cdot \varepsilon = 11.391$	Class 3	
			Class 4	
lower flange:	$\frac{b_{f,2} - t_w}{2 t_{f,2}} = 7.917$	$9 \cdot \varepsilon = 7.323$	Class 1	=> Class 2
		$10 \varepsilon = 8.136$	Class 2	
		$14 \cdot \varepsilon = 11.391$	Class 3	
			Class 4	

Cross section is Class 3 - elastic analysis

plastic section modulus: $W_{pl} := b_f \cdot t_f \cdot (H_{long} - t_f) + \frac{t_w \cdot h_w^2}{4} = 2048890 \cdot \text{mm}^3$ $\gamma_{M0} := 1$

elastic section modulus (from Robot Str. Analysis) : $W_{el} := 1282.6 \text{ cm}^3$

Moment resistance of cross girder:

$$f_y = 355 \cdot \frac{\text{N}}{\text{mm}^2}$$

$$M_{el.Rd} := \frac{W_{el} \cdot f_y}{\gamma_{M0}} = 455 \cdot \text{kN} \cdot \text{m}$$

$$\frac{M_{Ed}}{M_{el.Rd}} = 0.102 < 1 \quad \text{OK!}$$

Main girder:

Geometry:

I - profile: $H := 1700\text{mm}$

$t_w := 20\text{mm}$

$b_f := 400\text{mm}$

$t_f := 30\text{mm}$

$h_w := H - 2 \cdot t_f = 1.64 \times 10^3 \cdot \text{mm}$

$A_{\text{main}} := h_w \cdot t_w + 2b_f \cdot t_f = 56800 \cdot \text{mm}^2$

Span: $L := 18.67\text{m}$

Dinamic factor for main girder

$L_{\phi,\text{main}} := L = 18.67 \text{ m}$

$$\phi_{\text{main}} := \frac{2.16}{\sqrt{\frac{L_{\phi,\text{main}}}{\text{m}} - 0.2}} + 0.73 = 1.254$$

Case	Structural element	Determinant length L_{ϕ}
Main girders		
5.1	Simply supported girders and slabs (including steel beams embedded in concrete)	Span in main girder direction

Ref. EN1991-2 §6.4.5.3 Table 6.2

Loads:

Permanent load:

$G_{\text{main}} := A_{\text{main}} \cdot \rho \cdot g = 4.37 \cdot \frac{\text{kN}}{\text{m}}$ self weight of main girder

$G_{\text{cross}} := \frac{G_{\text{cross}}}{2} = 0.558 \cdot \frac{\text{kN}}{\text{m}}$ self weight of cross girder

$G_{\text{long}} = 1.057 \cdot \frac{\text{kN}}{\text{m}}$ self weight of railbearer

Rail self weight: $G_{\text{rail}} := 1 \frac{\text{kN}}{\text{m}}$

Traffic Load: LM71-22,5

$$Q_v := 125 \text{ kN}$$

$$q_v := 40 \frac{\text{kN}}{\text{m}}$$

$$Q_v := \phi_{\text{main}} \cdot Q_v = 157 \cdot \text{kN}$$

$$q_v := \phi_{\text{main}} \cdot q_v = 50 \cdot \frac{\text{kN}}{\text{m}}$$

Wind load:

height of the car: $H_{\text{car}} := 5 \text{ m}$

Mean wind load: $q_{\text{mean}} := 1 \text{ kPa}$

Longitudinal girder distance = gauge: $E := 1512 \text{ mm}$

$$f_{\text{wv}} := \frac{q_{\text{mean}} \cdot H_{\text{car}}^2}{2 \cdot E} = 8.267 \cdot \frac{\text{kN}}{\text{m}}$$

Load factors:

$$\gamma_G := 1.35 \quad \text{just permanent load}$$

L1.Eq610.a distributed load along girder axis

$$\gamma_G \cdot (G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}}) = 9.429 \cdot \frac{\text{kN}}{\text{m}}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_Q := 0.75$$

L2.Eq610.b

concentrated load at 'rail position'

$$F_2 := \gamma_Q \cdot Q_v \cdot 4 = 909 \cdot \text{kN}$$

distributed load along girder axis

$$f_{2i} := \gamma_G \cdot (G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}}) + \gamma_Q \cdot q_v + \gamma_{\text{wind}} \cdot \psi_{0i} \cdot f_w = 90.772 \cdot \frac{\text{kN}}{\text{m}}$$

$$\gamma_G := 1.25 \quad \gamma_Q := 1.45 \quad \gamma_{\text{wind}} := 1.5 \quad \psi_{0i} := 0.8$$

L3.Eq610.b

concentrated load at 'rail position'

$$F_3 := \gamma_Q \cdot \psi_{0i} \cdot Q_v \cdot 4 = 727 \cdot \text{kN}$$

distributed load along girder axis

$$f_3 := \gamma_G \cdot (G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}}) + \gamma_Q \cdot \psi_{0i} \cdot q_v + \gamma_{\text{wind}} \cdot f_w = 79.324 \cdot \frac{\text{kN}}{\text{m}}$$

I only calculate the design moment for L2 load combination (the most relevant one)

I assume that the main girder is a simply supported beam.

$$M_{Ed} := \frac{f_2 \cdot L^2}{8} + \frac{F_2 \cdot L}{4} = 8199 \cdot \text{kN} \cdot \text{m}$$

Cross section resistance:

Cross section classification:

web:	$\frac{h_w}{t_w} = 82$	$72 \cdot \epsilon = 58.58$	Class 1	
		$83 \cdot \epsilon = 67.53$	Class 2	=> Class 3
		$124 \cdot \epsilon = 100.888$	Class 3	
flange:	$\frac{b_f - t_w}{t_f} = 6.333$	$9 \cdot \epsilon = 7.323$	Class 1	
		$10 \epsilon = 8.136$	Class 2	=> Class 1
		$14 \cdot \epsilon = 11.391$	Class 3	

Cross section is Class 3 - elastic analysis

plastic section modulus: $W_{pl} := b_f \cdot t_f \cdot (H - t_f) + \frac{t_w \cdot h_w^2}{4} = 33488000 \cdot \text{mm}^3$

elastic section modulus:
$$W_{el} := \frac{b_f \cdot H^2}{6} - \frac{(b_f - t_w) \cdot h_w^3}{6 \cdot H} = 28337380 \cdot \text{mm}^3$$

Moment resistance of cross girder:

$$\gamma_{M0} := 1$$

$$M_{el.Rd} := \frac{W_{el} \cdot f_y}{\gamma_{M0}} = 10060 \cdot \text{kN} \cdot \text{m}$$

$$\frac{M_{Ed}}{M_{el.Rd}} = 0.815 < 1 \quad \text{OK!}$$

Deflection of main girder:

second moment of area:
$$I := \frac{h_w^3 \cdot t_w}{12} + \left(\frac{b_f}{12} \right) \cdot (H^3 - h_w^3) = 2.409 \times 10^{10} \cdot \text{mm}^4$$

modulus of elasticity:
$$E_a := 210000 \frac{\text{N}}{\text{mm}^2}$$

permanent characteristic:
$$g_k := G_{\text{cross}} + G_{\text{main}} + G_{\text{long}} + G_{\text{rail}} = 6.984 \cdot \frac{\text{kN}}{\text{m}}$$

variable characteristic:
$$q_k := q_v + f_w = 58.434 \cdot \frac{\text{kN}}{\text{m}}$$

$$Q_k := 4Q_v = 627.08 \cdot \text{kN}$$

the calculation of deflection is an approximation on the safe side

$$\delta_{\text{max}} := \frac{5 \cdot (g_k + q_k) \cdot L^4}{384 \cdot E_a \cdot I} + \frac{Q_k \cdot L^3}{48 \cdot E_a \cdot I} = 37.27 \cdot \text{mm} < \frac{L}{400} = 46.675 \cdot \text{mm}$$

Total weight of structure:

$$n_{\text{cross}} := \text{ceil} \left(\frac{L}{L_{\text{cross}}} \right) = 11$$

$$A_{\text{cross}} \cdot l_{\text{cross}} \cdot \rho \cdot n_{\text{cross}} = 5.979 \times 10^3 \text{ kg}$$

$$n_{\text{long}} := 2$$

$$A_{\text{long}} \cdot L \cdot \rho \cdot n_{\text{long}} = 4.027 \times 10^3 \text{ kg}$$

$$n_{\text{main}} := 2$$

$$A_{\text{main}} \cdot L \cdot \rho \cdot n_{\text{main}} = 1.665 \times 10^4 \text{ kg}$$

Buckling support girder:

Geometry:

$$\begin{aligned} \text{l - profile: } h_b &:= 246 \text{ mm} \\ t_{w,b} &:= 10 \text{ mm} \\ b_{f,b} &:= 120 \text{ mm} \\ t_{f,b} &:= 13 \text{ mm} \\ h_{w,b} &:= h_b - 2 \cdot t_{f,b} = 220 \cdot \text{mm} \end{aligned}$$

$$A_{\text{buckl}} := h_{w,b} \cdot t_{w,b} + 2b_{f,b} \cdot t_{f,b} = 5320 \cdot \text{mm}^2$$

$$l_{\text{buckl}} := E = 1.512 \text{ m}$$

$$n_{\text{buckl}} := n_{\text{cross}} - 1 = 10$$

Wind bracing:

$$A_w := 102 \text{ mm} \cdot 13 \text{ mm} = 1.326 \times 10^{-3} \text{ m}^2$$

$$L_w := 5466 \text{ mm}$$

$$n_w := 10$$

$$\begin{aligned} G_{\text{TOT}} := & A_{\text{main}} \cdot L \cdot \rho \cdot n_{\text{main}} + A_{\text{long}} \cdot L \cdot \rho \cdot n_{\text{long}} + A_{\text{cross}} \cdot l_{\text{cross}} \cdot \rho \cdot n_{\text{cross}} \dots = 27.856 \cdot \text{tonne} \\ & + A_{\text{buckl}} \cdot l_{\text{buckl}} \cdot \rho \cdot n_{\text{buckl}} + A_w \cdot L_w \cdot \rho \cdot n_w \end{aligned}$$

$$G_{\text{TOT}} \cdot g = 272.99 \cdot \text{kN}$$

$$\text{Side walk: } g_{\text{sw}} := 80 \frac{\text{kg}}{\text{m}}$$

$$L = 18.67 \text{ m}$$

$$G_{\text{TOT}} \cdot g + g_{\text{sw}} \cdot L \cdot g = 287.62 \cdot \text{kN}$$

$$G_{\text{TOT}} + g_{\text{sw}} \cdot L = 29349.28 \cdot \text{kg}$$

APPENDIX 3

Connection Calculation Report - Crossgirder-railbearer

Material:

Bolt class: 4.6

$$f_{yb} := 240 \frac{N}{mm^2} \qquad f_{ub} := 400 \frac{N}{mm^2}$$

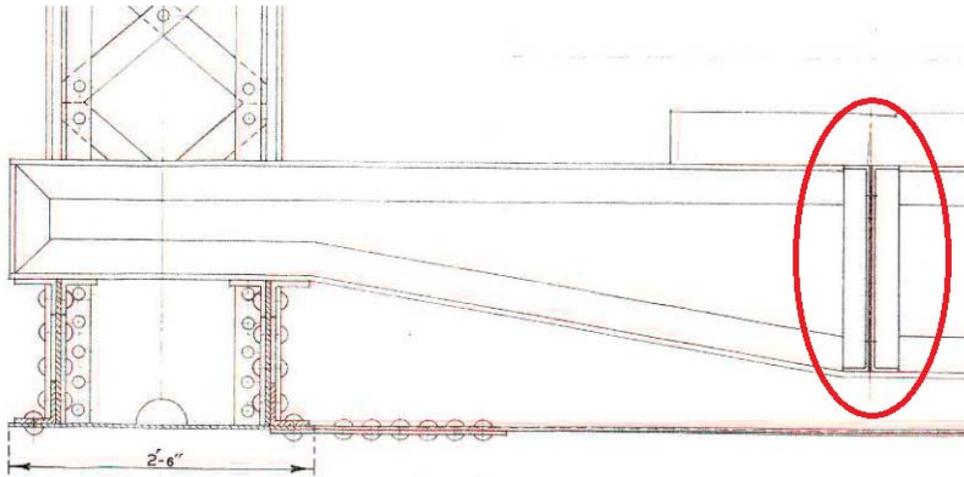
Ref. EN1993-1-8
§3.1.1
Table 3.1

Steel grade: S235

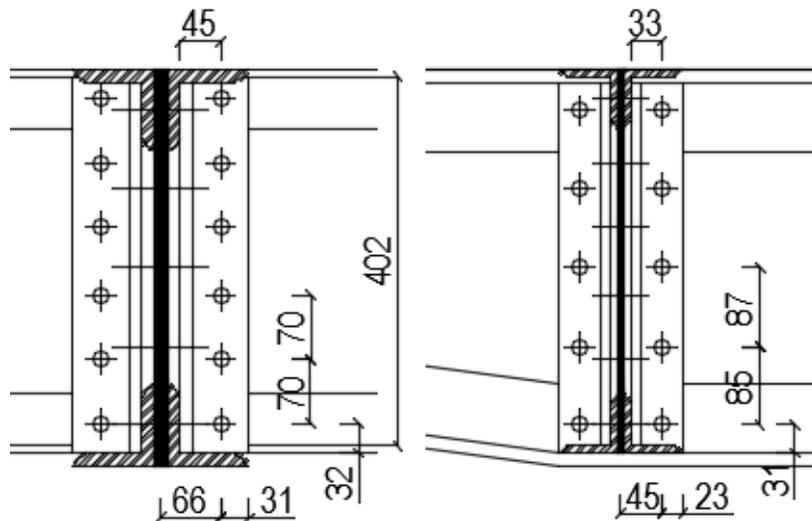
$$f_y := 235 \frac{N}{mm^2} \qquad f_u := 360 \frac{N}{mm^2}$$

Ref. EN1993-1-1
§3.2.3
Table 3.1

Geometry of joint: The geometrical data are assumptions, for achieving an accurate results, a site inspection is needed to gather the missing information.



Connection between cross girder and railbearer



Supported beam side

Supporting beam side

$$d := 20\text{mm}$$

$$A_b := \frac{d^2 \cdot \pi}{4} = 314 \cdot \text{mm}^2 \quad \text{the gross cross section of the bolt}$$

$$d_0 := d + 2\text{mm} = 22 \cdot \text{mm}$$

$$p_1 := 70\text{mm}$$

$z := 66\text{mm}$ is the transverse distance from the face of the supporting element to the centre of the bolt group

$$n_b := 6$$

Partial safety factor for joint:

$$\gamma_{M2} := 1.25 \quad \text{Ref. EN1993-1-8 §2.2 Table 2.1}$$

$$\gamma_{M0} := 1 \quad \text{Ref. EN1993-1-1 §6.1 Note 2B}$$

Supported beam side:

Shear resistance of bolts Basic requirement: $V_{Ed} \leq V_{Rd}$

$$V_{Rd} = \frac{2 \cdot n_b \cdot F_{v,Rd}}{\sqrt{(1 + \alpha n_b)^2 + (\beta \cdot n_b)^2}}$$

$$F_{v,Rd} = \frac{\alpha_v \cdot f_{ub} \cdot A}{\gamma_{M2}} \quad \text{Shear resistance per shear plane}$$

Ref. EN1993-1-8
§3.6.1
Table 3.4

for classes 4.6~ 5.6 and 8.8:

$$\alpha_v = 0,6$$

$$\Rightarrow \alpha_v := 0.6$$

- for classes 4.8, 5.8, 6.8 and 10.9:

$$\alpha_v = 0,5$$

For a single vertical line of bolts:

$$\alpha := 0$$

$$\beta = \frac{6 \cdot z}{n_1 \cdot (n_1 + 1) \cdot p_1}$$

$$n_1 := n_b = 6$$

$$\beta := \frac{6 \cdot z}{n_1 \cdot (n_1 + 1) \cdot p_1} = 0.135$$

$$F_{v.Rd} := \frac{\alpha_v \cdot f_{ub} \cdot A_b}{\gamma_{M2}} = 60.319 \cdot \text{kN}$$

$$V_{v.Rd} := \frac{2 \cdot n_b \cdot F_{v.Rd}}{\sqrt{(1 + \alpha \cdot n_b)^2 + (\beta \cdot n_b)^2}} = 562.962 \cdot \text{kN}$$

Bearing resistance of bolts on the angle cleats Basic requirement: $V_{Ed} \leq V_{Rd}$

$$V_{Rd} = \frac{2 \cdot n_b}{\sqrt{\left(\frac{1 + \alpha \cdot n_b}{F_{b.ver.Rd}}\right)^2 + \left(\frac{\beta \cdot n_b}{F_{b.hor.Rd}}\right)^2}}$$

The vertical bearing resistance of a single bolt on the angle cleat is as follows:

$$F_{b.ver.Rd} = \frac{k_1 \cdot \alpha_b \cdot f_{u.ac} \cdot d \cdot t_{ac}}{\gamma_{M2}}$$

Ref. EN1993-1-8
§3.6.1
Table 3.4

$$e_2 := 31 \text{mm} \quad e_1 := 32 \text{mm} \quad t_{ac} := 11 \text{mm}$$

$$k_{1.ver} := \min\left(2.8 \cdot \frac{e_2}{d_0} - 1.7, 2.5\right) = 2.245$$

$$f_{u.ac} := f_u = 360 \cdot \text{MPa}$$

$$\alpha_{b.ver} := \min\left(\frac{e_1}{3 \cdot d_0}, \frac{p_1}{3 \cdot d_0} - \frac{1}{4}, \frac{f_{ub}}{f_{u.ac}}, 1\right) = 0.485$$

$$F_{b.ver.Rd} := \frac{k_{1.ver} \cdot \alpha_{b.ver} \cdot f_{u.ac} \cdot d \cdot t_{ac}}{\gamma_{M2}} = 68.98 \cdot \text{kN}$$

The horizontal bearing resistance of a single bolt on the angle cleat is as follows:

$$F_{b.hor.Rd} = \frac{k_1 \cdot \alpha_b \cdot f_{u.ac} \cdot d \cdot t_{ac}}{\gamma_{M2}}$$

Ref. EN1993-1-8
§3.6.1
Table 3.4

$$k_{1.hor} := \min\left(2.8 \cdot \frac{e_1}{d_0} - 1.7, 1.4 \cdot \frac{p_1}{d_0} - 1.7, 2.5\right) = 2.373$$

$$\alpha_{b,hor} := \min\left(\frac{e_2}{3 \cdot d_0}, \frac{f_{ub}}{f_{u,ac}}, 1\right) = 0.47$$

$$F_{b,hor.Rd} := \frac{k_{1,hor} \cdot \alpha_{b,hor} \cdot f_{u,ac} \cdot d \cdot t_{ac}}{\gamma_{M2}} = 70.612 \cdot \text{kN}$$

$$V_{b,Rd} := \frac{2 \cdot n_b}{\sqrt{\left(\frac{1 + \alpha \cdot n_b}{F_{b,ver.Rd}}\right)^2 + \left(\frac{\beta \cdot n_b}{F_{b,hor.Rd}}\right)^2}} = 650 \cdot \text{kN}$$

Bearing resistance of bolts on the beam web Basic requirement: $V_{Ed} \leq V_{Rd}$

$$e_{2,w} := 45 \text{mm} \quad t_w := 14 \text{mm}$$

$$V_{Rd} = \frac{n_b}{\sqrt{\left(\frac{1 + \alpha \cdot n_b}{F_{b,ver.Rd}}\right)^2 + \left(\frac{\beta \cdot n_b}{F_{b,hor.Rd}}\right)^2}}$$

The vertical bearing resistance:

$$F_{b,ver.Rd.2} = \frac{k_1 \cdot \alpha_b \cdot f_{u,w} \cdot d \cdot t_w}{\gamma_{M2}}$$

Ref. EN1993-1-8
§3.6.1
Table 3.4

$$k_{1,ver.2} := \min\left(2.8 \cdot \frac{e_{2,w}}{d_0} - 1.7, 2.5\right) = 2.5$$

$$f_{u,w} := f_u = 360 \cdot \text{MPa}$$

$$\alpha_{b,ver.2} := \min\left(\frac{e_1}{3 \cdot d_0}, \frac{p_1}{3 \cdot d_0} - \frac{1}{4}, \frac{f_{ub}}{f_{u,w}}, 1\right) = 0.485$$

$$F_{b,ver.Rd.2} := \frac{k_{1,ver.2} \cdot \alpha_{b,ver.2} \cdot f_{u,w} \cdot d \cdot t_w}{\gamma_{M2}} = 97.745 \cdot \text{kN}$$

The horizontal bearing resistance:

$$F_{b,hor.Rd.2} = \frac{k_1 \cdot \alpha_b \cdot f_{u,ac} \cdot d \cdot t_w}{\gamma_{M2}}$$

Ref. EN1993-1-8
§3.6.1
Table 3.4

$$k_{1,hor.2} := \min\left(2.8 \cdot \frac{e_1}{d_0} - 1.7, 1.4 \cdot \frac{p_1}{d_0} - 1.7, 2.5\right) = 2.373$$

$$\alpha_{b,hor.2} := \min\left(\frac{e_{2,w}}{3 \cdot d_0}, \frac{f_{ub}}{f_{u,w}}, 1\right) = 0.682$$

$$F_{b,hor.Rd.2} := \frac{k_{1,hor.2} \cdot \alpha_{b,hor.2} \cdot f_{u,w} \cdot d \cdot t_w}{\gamma_{M2}} = 130.457 \cdot \text{kN}$$

$$V_{b.Rd.2} := 2 \cdot \frac{n_b}{\sqrt{\left(\frac{1 + \alpha \cdot n_b}{F_{b.ver.Rd.2}}\right)^2 + \left(\frac{\beta \cdot n_b}{F_{b,hor.Rd.2}}\right)^2}} = 1003 \cdot \text{kN}$$

Multiplied by two, because the bearing resistance of the web works against half of the design shear force.

Supporting beam side:

Basic requirement:

$$V_{Ed} \leq F_{Rd}$$

$$F_{Rd} = \begin{cases} \sum_n F_{b,Rd} & \text{if } \max(F_{b,Rd}) \leq F_{v,Rd} \\ n_s \cdot \min(F_{b,Rd}) & \text{if } \min(F_{b,Rd}) \leq F_{v,Rd} \leq \max(F_{b,Rd}) \\ 0.8 \cdot n_s \cdot F_{v,Rd} & \text{if } F_{v,Rd} \leq \min(F_{b,Rd}) \end{cases}$$

Ref. EN1993-1-8
§3.7 (1)

Shear resistance of bolts:

$$F_{v,Rd} = 60 \cdot \text{kN}$$

Bearing resistance of bolts on the angle cleats

$$F_{b,Rd} = \frac{k_1 \cdot \alpha_b \cdot f_{u,ac} \cdot d \cdot t_{ac}}{\gamma_{M2}}$$

Ref. EN1993-1-8
§3.6.1
Table 3.4

$$e_{2,w} := 23\text{mm} \quad e_{1,w} := 31\text{mm} \quad p_1 := 85\text{mm}$$

For edge bolts: $k_{1,ac} := \min\left(2.8 \cdot \frac{e_2}{d_0} - 1.7, 2.5\right) = 1.227$

For end bolts: $\alpha_{b,ac,end} := \min\left(\frac{e_1}{3 \cdot d_0}, \frac{f_{ub}}{f_{u,ac}}, 1\right) = 0.47$

For inner bolts: $\alpha_{b,ac,inn} := \min\left(\frac{p_1}{3 \cdot d_0} - \frac{1}{4}, \frac{f_{ub}}{f_{u,ac}}, 1\right) = 1$

For end bolts: $F_{b,Rd,end} := \frac{k_{1,ac} \cdot \alpha_{b,ac,end} \cdot f_{u,ac} \cdot d \cdot t_{ac}}{\gamma_{M2}} = 36.524 \cdot \text{kN}$

For inner bolts: $F_{b,Rd,inn} := \frac{k_{1,ac} \cdot \alpha_{b,ac,inn} \cdot f_{u,ac} \cdot d \cdot t_{ac}}{\gamma_{M2}} = 77.76 \cdot \text{kN}$

$F_{b,Rd,min} := \min(F_{b,Rd,end}, F_{b,Rd,inn}) = 36.524 \cdot \text{kN}$

$F_{b,Rd,max} := \max(F_{b,Rd,end}, F_{b,Rd,inn}) = 77.76 \cdot \text{kN}$

$n_{b,2} := 5$ number of bolts on supporting beam side

$n_s := 2 \cdot n_{b,2} = 10$

$$F_{Rd} := \begin{cases} F_{b,Rd,end} + F_{b,Rd,inn} & \text{if } F_{b,Rd,max} \leq F_{v,Rd} \\ n_s \cdot F_{b,Rd,min} & \text{if } F_{b,Rd,min} \leq F_{v,Rd} \leq F_{b,Rd,max} \\ 0.8 \cdot n_s \cdot F_{v,Rd} & \text{if } F_{v,Rd} \leq F_{b,Rd,min} \end{cases} = 365 \cdot \text{kN}$$

Supported beam side:

$e_{2,w} := 31\text{mm}$ $e_{1,w} := 32\text{mm}$ $p_{1,w} := 70\text{mm}$

Shear resistance of the angle cleats

Basic requirement: $V_{Ed} \leq V_{Rd,min}$

$V_{Rd,min} = \min(V_{Rd,g}, V_{Rd,n}, V_{Rd,b})$

Shear resistance of gross section

$$V_{Rd,g} = 2 \cdot \frac{h_{ac} \cdot t_{ac}}{1.27} \cdot \frac{f_{y,ac}}{\sqrt{3} \cdot \gamma_{M0}}$$

Note: The coefficient 1,27 takes into account the reduction in shear resistance due to the presence of the nominal in-plane bending which produces tension in the bolts

$$h_{ac} := 402\text{mm} \quad t_{ac} = 11\text{mm} \quad f_{y.ac} := f_y = 235\text{MPa}$$

$$V_{Rd.g} := 2 \cdot \frac{h_{ac} \cdot t_{ac}}{1.27} \cdot \frac{f_{y.ac}}{\sqrt{3} \cdot \gamma_{M0}} = 945\text{ kN}$$

Shear resistance of net section

$$V_{Rd.n} = 2 \cdot A_{v.net} \cdot \frac{f_{u.ac}}{\sqrt{3} \cdot \gamma_{M2}}$$

$$A_{v.net} := t_{ac} \cdot (h_{ac} - n_1 \cdot d_0) = 2970\text{ mm}^2$$

$$V_{Rd.n} := 2 \cdot A_{v.net} \cdot \frac{f_{u.ac}}{\sqrt{3} \cdot \gamma_{M2}} = 988\text{ kN}$$

Block tearing resistance

$$V_{Rd.b} = 2 \cdot \left(\frac{0.5 \cdot f_{u.ac} \cdot A_{nt}}{\gamma_{M2}} + \frac{f_{y.ac} \cdot A_{nv}}{\sqrt{3} \cdot \gamma_{M0}} \right)$$

Ref.
EN1993-1-8
§3.10.2 (2)

$$A_{nt} := t_{ac} \cdot (e_2 - 0.5 \cdot d_0)$$

$$A_{nv} := t_{ac} \cdot [h_{ac} - e_1 - (n_1 - 0.5) \cdot d_0]$$

$$V_{Rd.b} := 2 \cdot \left(\frac{0.5 \cdot f_{u.ac} \cdot A_{nt}}{\gamma_{M2}} + \frac{f_{y.ac} \cdot A_{nv}}{\sqrt{3} \cdot \gamma_{M0}} \right) = 807\text{ kN}$$

$$V_{Rd.min} := \min(V_{Rd.g}, V_{Rd.n}, V_{Rd.b}) = 807\text{ kN}$$

Supporting beam side:

Shear resistance of the angle cleats

Basic requirement: $V_{Ed} \leq V_{Rd.min}$

$$V_{Rd.min} = \min(V_{Rd.g}, V_{Rd.n}, V_{Rd.b})$$

Shear resistance of gross section

$$V_{Rd.g} = 2 \cdot \frac{h_{ac} \cdot t_{ac}}{1.27} \cdot \frac{f_{y.ac}}{\sqrt{3} \cdot \gamma_{M0}}$$
$$V_{Rd.g.2} := 2 \cdot \frac{h_{ac} \cdot t_{ac}}{1.27} \cdot \frac{f_{y.ac}}{\sqrt{3} \cdot \gamma_{M0}} = 945 \cdot \text{kN}$$

Shear resistance of net section

$$V_{Rd.n} = 2 \cdot A_{v.net} \cdot \frac{f_{u.ac}}{\sqrt{3} \cdot \gamma_{M2}}$$
$$A_{v.net.2} := t_{ac} \cdot (h_{ac} - n_{b.2} \cdot d_0) = 3212 \cdot \text{mm}^2$$
$$V_{Rd.n.2} := 2 \cdot A_{v.net.2} \cdot \frac{f_{u.ac}}{\sqrt{3} \cdot \gamma_{M2}} = 1068 \cdot \text{kN}$$

Block tearing resistance

$$V_{Rd.b} = 2 \cdot \left(\frac{0.5 \cdot f_{u.ac} \cdot A_{nt}}{\gamma_{M2}} + \frac{f_{y.ac} \cdot A_{nv}}{\sqrt{3} \cdot \gamma_{M0}} \right)$$
$$A_{nt.2} := t_{ac} \cdot (e_2 - 0.5 \cdot d_0)$$
$$A_{nv.2} := t_{ac} \cdot [h_{ac} - e_1 - (n_{b.2} - 0.5) \cdot d_0]$$
$$V_{Rd.b.2} := 2 \cdot \left(\frac{0.5 \cdot f_{u.ac} \cdot A_{nt.2}}{\gamma_{M2}} + \frac{f_{y.ac} \cdot A_{nv.2}}{\sqrt{3} \cdot \gamma_{M0}} \right) = 872 \cdot \text{kN}$$
$$V_{Rd.min.2} := \min(V_{Rd.g.2}, V_{Rd.n.2}, V_{Rd.b.2}) = 872 \cdot \text{kN}$$

Ref.
EN1993-1-8
§3.10.2 (2)

Shear resistance of the beam web

Shear and block tearing resistance

Basic requirement: $V_{Ed} \leq V_{Rd.min}$

$$V_{Rd.min} = \min(V_{Rd.g}, V_{Rd.n}, V_{Rd.b})$$

Shear resistance of gross section

$$V_{Rd.g.wb} = A_{v.wb} \cdot \frac{f_{y.b}}{\sqrt{3} \cdot \gamma_{M0}}$$

$$f_{y,b} := f_y = 235 \cdot \text{MPa}$$

$$h_w := h_{ac} = 402 \cdot \text{mm} \quad t_w = 14 \cdot \text{mm}$$

$$A_{v,wb} := h_w \cdot t_w = 5628 \cdot \text{mm}^2$$

$$V_{Rd,g,wb} := A_{v,wb} \cdot \frac{f_{y,b}}{\sqrt{3} \cdot \gamma_{M0}} = 763.592 \cdot \text{kN}$$

Shear resistance of net section

$$V_{Rd,n,wb} = A_{v,wb,net} \cdot \frac{f_{u,b}}{\sqrt{3} \cdot \gamma_{M0}}$$

$$A_{v,wb,net} := A_{v,wb} - n_b \cdot d_0 \cdot t_w$$

$$f_{u,b} := f_u = 360 \cdot \text{MPa}$$

$$V_{Rd,n,wb} := A_{v,wb,net} \cdot \frac{f_{u,b}}{\sqrt{3} \cdot \gamma_{M0}} = 785.658 \cdot \text{kN}$$

Block tearing resistance

$$V_{Rd,b} = 2 \cdot \left(\frac{0.5 \cdot f_{u,ac} \cdot A_{nt}}{\gamma_{M2}} + \frac{f_{y,ac} \cdot A_{nv}}{\sqrt{3} \cdot \gamma_{M0}} \right)$$

$$A_{nt,wb} := t_w \cdot (e_{2,w} - 0.5 \cdot d_0) = 476 \cdot \text{mm}^2$$

$$A_{nv,wb} := t_w \cdot [e_1 + (n_1 - 1) \cdot p_1 - (n_1 - 0.5) \cdot d_0] = 3.654 \times 10^3 \cdot \text{mm}^2$$

$$V_{Rd,b,wb} := 2 \cdot \left(\frac{0.5 \cdot f_{u,b} \cdot A_{nt,wb}}{\gamma_{M2}} + \frac{f_{y,b} \cdot A_{nv,wb}}{\sqrt{3} \cdot \gamma_{M0}} \right) = 1129 \cdot \text{kN}$$

$$V_{Rd,min,wb} := \min(V_{Rd,g,wb}, V_{Rd,n,wb}, V_{Rd,b,wb}) = 764 \cdot \text{kN}$$

Ref.
EN1993-1-8
§3.10.2 (2)

Summary of design checks:

Shear resistance:

Bolt group design

Supported beam side

Shear resistance of bolts: $V_{v,Rd} = 563 \cdot \text{kN}$

Bearing resistance of bolts on angle cleats: $V_{b,Rd} = 650 \cdot \text{kN}$

Bearing resistance of bolts on the beam web: $V_{b,Rd.2} = 1003 \cdot \text{kN}$

Supporting beam side

Resistance: $F_{Rd} = 365 \cdot \text{kN}$

Shear resistance of the angle cleats

Supported beam side

Shear resistance: $V_{Rd.min} = 807 \cdot \text{kN}$

Supporting beam side

Shear resistance: $V_{Rd.min.2} = 872 \cdot \text{kN}$

Shear resistance of the beam web

Shear and block tearing resistance

Shear resistance: $V_{Rd.min.wb} = 764 \cdot \text{kN}$

$$V_{Rd} := \min(V_{v,Rd}, V_{b,Rd}, V_{b,Rd.2}, V_{Rd.min}, V_{Rd.min.2}, V_{Rd.min.wb}, F_{Rd}) = 365 \cdot \text{kN}$$

$V_{Ed} := 468.8\text{kN}$ From Robot Structural Analysis

$\frac{V_{Ed}}{V_{Rd}} = 1.284 > 1$ The joint is failing due to the shear design force and the critical failure mode is the bearing resistance of the bolts on the angle cleats on supporting beam side.

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